# Multi-objective no-wait flow-shop scheduling with a memetic algorithm based on differential evolution 

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#### Abstract

In this paper, a memetic algorithm (MA) based on differential evolution (DE), namely MADE, is proposed for the multi-objective no-wait flow-shop scheduling problems (MNFSSPs). Firstly, a largest-order-value rule is presented to convert individuals in DE from real vectors to job permutations so that the DE can be applied for solving flowshop scheduling problems (FSSPs). Secondly, the DE-based parallel evolution mechanism is applied to perform effective exploration, and several local searchers developed according to the landscape of multi-objective FSSPs are applied to emphasize local exploitation. Thirdly, a speed-up computing method is developed based on the property of the no-wait FSSPs. In addition, the concept of Pareto dominance is used to handle the updating of solutions in sense of multi-objective optimization. Due to the well balance between DE-based global search and problem-dependent local search as well as the utilization of the speed-up evaluation, the MNFSSPs can be solved effectively and efficiently. Simulation results and comparisons demonstrate the effectiveness and efficiency of the proposed MADE.


[^0]Keywords Multi-objective no-wait flow-shop scheduling • Differential evolution • Memetic algorithm • Local search • Exploration and exploitation

## 1 Introduction

Production scheduling is an important issue faced daily both in the manufacturing systems and the service industries. So, it is necessary to develop effective and efficient advanced manufacturing and scheduling technologies and approaches (Stadtler 2005; Dimopoulos and Zalzala 2000; Wang 2003). The flow shop scheduling problem (FSSP) is a class of widely studied scheduling problems. It represents nearly a quarter of manufacturing systems, assembly lines and information service facilities nowadays (Pinedo 2002) and is considered as being difficult to solve (Garey and Johnson 1979; Baker 1974). In many FSSPs, there exists a constraint that once the processing of a job begins, subsequent processing must be performed without waiting between or on consecutive machines. Such a FSSP is termed as no-wait FSSP (NFSSP). Some typical situations are encountered in metal, plastic, chemical and pharmaceutical industries. For example, a plastic product requires to be processed through a continuous sequence of operations to prevent degradation. According to the research work by Garey and Johnson (1979), the NFSSP is NP-hard.

Due to its significance both in theory and industrial applications, the NFSSP has been studied by many researchers. Historically, NFSSP has been primarily treated by the branch-and-bound method (Van Deman and Baker 1974), constructive methods (Bonney and Gundry 1976; King and Spachis 1980; Gangadharan and Rajendran 1993; Rajendran 1994). Recently, metaheuristic methods have attracted wide research attention, including such topics as genetic algorithm
(GA) (Chen et al. 1996; Kumar et al. 2000; Aldowaisan and Allahverdi 2003), simulated annealing (SA) algorithm (Aldowaisan and Allahverdi 2003), tabu search (TS) algorithm (Grabowski and Pempera 2005), descending search (DS) algorithm (Grabowski and Pempera 2005), hybrid particle swarm optimization (HPSO) algorithm (Liu et al. 2007). An early comprehensive survey of the NFSSP can be found in Hall and Sriskandarajah (1996). As we know, most real scheduling problems naturally involve the optimization of multiple objectives. Up to now, few researchers have studied multi-objective NFSSPs (MNFSSPs). Allahverdi and Aldowaisan (2004) presented two hybrid algorithms based on SA and GA to minimize a weighted sum of makespan and maximum lateness. Tavakkoli-Moghaddam et al. (2007) addressed the MNFSSP that minimizes both the weighted mean completion time and weighted mean tardiness, and developed a hybrid multi-objective immune algorithm (IA) to obtain Optimal Pareto solution for such problem.

Over the past 15 years, memetic algorithms (MAs) have been a hot topic in the fields of both computer science and operational research (Reeves and Yamada 1998; Murata et al. 1996; Ong et al. 2006; Hart et al. 2004). It assumes that combining the features of different methods in a complementary fashion may result in more robust and effective optimization tools. MAs belong to the class of evolutionary algorithms (EAs) that combine the global and local search by using an EA to execute exploration while the local search method executes exploitation, which are inspired by Darwinian principles of natural evolution and Dawkins' notion of a meme defined as a unit of cultural evolution that is capable of local refinements. Some recent work demonstrates that MAs (sometimes called hybrid EAs) can yield promising results for solving combinatorial and nonlinear optimization problems (Tang et al. 2007; Zhou et al. 2007; Ong and Keane 2004) and engineering problems (Caponio et al. 2007; Ong and Keane 2004). In MAs, studies (Hart et al. 2004; Zhu et al. 2007; Ishibuchi et al. 2003) have been focused on how to achieve a reasonable combination of global search and local search, and how to make a good balance between exploration and exploitation. As for multiobjective FSSPs, Ishibuchi and Murata (1998) firstly devised a multi-objective memetic algorithm (IMMOGLS) by combining GA with the local search method, which used a scalar fitness function with random weights to guide the evolution process of GA-based search and local search to find optimal Pareto front. Jaszkiewicz (2002) implemented another genetic local search algorithm (JMOGLS), which was similar to IMMOGLS. The main difference lies in the selection mechanism of parents. Ishibuchi et al. (2003) proposed a modified IMMOGLS (IMMOGLS2) by adopting a more reasonable local searcher in multi-objective sense. Moreover, the impact of balance between global search and local search was analyzed. Arroyo and Armentano (2005)
conceived a multi-objective GA (AAMOGLS), in which the concept of Pareto dominance is used to rank the population and assign suitable fitness values to all the individuals. Subsequently, a local searcher based on Pareto dominance was applied to perform the exploitation. However, the research work about MAs for NFSSPs and MNFSSPs is very scarce. Liu et al. (2007) proposed an effective memetic algorithm based on particle swarm optimization (PSO) algorithm to minimize makespan, where several local searchers or memes with adaptive learning strategy were incorporated into PSO. Tavakkoli-Moghaddam et al. (2007) implemented a hybrid multi-objective IA to minimize both the weighted mean completion time and weighted mean tardiness, where two local searchers, namely bacterial mutation and gene transfer, were applied to improve the quality of some selected individuals (i.e., antibodies).

Differential evolution (DE) is a novel population-based evolutionary mechanism recently proposed for global optimization over continuous spaces (Storn and Price 1997). Despite DE's structure simplicity, the key evolutionary operators of mutation and crossover are very efficient, which allows the search behavior of each individual to self-adapting. Due to its ease of use, fast convergence and robustness, DE has gained wide application in a variety of fields (Ilonen et al. 2003; Chang and Wu 2005; Feoktistov 2006; Price and Storn 2007). Because DE's individual is a real vector, it is difficult to directly present feasible solutions to combinatorial optimization problems (COPs). Thus, the research work of DE for scheduling problems is quite limited. Recently, Tasgetiren et al. (2004) implemented an encoding scheme to convert the continuous values of individuals in DE to job permutations and incorporated Interchange-based local searcher into DE to minimize the makespan criterion of FSSPs. Onwubolu and Davendra (2006) developed a DE-based heuristic to solve FSSPs with the objectives of makespan, mean flowtime, and total tardiness. Nearchou and Omirou (2006) designed a stochastic method based on DE to deal with three classic NP-hard scheduling problems: the flow-shop scheduling problem, the single-machine total weighted tardiness problem, and the single machine common due date scheduling problem. Nearchou (2008) presented a DE-based algorithm to address the common due date early/tardy job scheduling problem on a single machine, which could find new upper bounds to nearly $60 \%$ of the testing benchmark problems. As for multi-objective scheduling problems, Qian et al. (2008) proposed a memetic algorithm based on DE for multi-objective job shop scheduling problems (MJSSPs), which used several memes and adopted an adaptive Meta-Lamarckian strategy to dynamically decide which meme to be selected to emphasize exploitation in each generation. To the best of our knowledge, there are few other published papers on DE for shop scheduling, and especially there is no published paper on DE for the multi-objective no-wait FSSPs.

In this paper, we will devise a memetic algorithm based on DE (MADE) by combining DE with several problem dependent memes for the no-wait multi-objective FSSPs. The motivation of MADE is based on the 'no free lunch theory' (Wolpert and Macready 1997). That is, any algorithm without adopting the domain knowledge of problems is only equal to a kind of random search, and it is impossible to obtain excellent performance on special problems. Thus, when designing MADE, we fully considered some structure information of MNFSSPs. For FSSPs, the solution space landscape induced by some specific neighborhoods (i.e., Insert, Interchange, Swap, etc.) has a "big valley," where local optima tend to be relatively close to each other and to the global optima at the big valley's bottom part (Reeves and Yamada 1998; Reeves 1999). And the size of the bottom region of the big valley containing global or satisfactory local optima is considerably small with respect to the whole valley. However, the number of solutions in the bottom region is also so large that it is unlikely to apply a total search (Nowicki and Smutnicki 2006). For MNFSSPs, different objective induces different shape of big valley. Since the objectives are usually not positively correlated, it is difficult for a solution to simultaneously reach the bottom regions of all big valleys. That is to say, the effectiveness of searching in the different big valleys directly determines the performance of MADE. Fortunately, the DE's mutation operation is quite unique, which is driven by the differences between contemporary population members. This allows the search behavior of each individual to self-tune during the search process, and gives an appropriate search direction to guide the search to find the global optima. So, in our MADE for MNFSSPs, DE is applied to find the promising solutions or regions over the solution space, and three efficient memes based on the landscape of FSSP are conceived to exploit the solution space from those regions and to guide the population to the bottom regions of big valleys, where Optimal Pareto solutionsor satisfactory Pareto solutionsare contained. In short, firstly, a largest-order-value (LOV) rule is proposed to map the continuous values of individuals in DE to job permutations so as to make DE suitable for solving FSSPs; secondly, the DE-based search is applied for exploration in a parallel framework, while several problem-dependent memes are utilized to emphasize exploitation; thirdly, a speed-up computing method base on the property of the NFSSPs is developed to calculate the objective functions efficiently. Simulation results and comparisons based on the testing benchmark instances validate the effectiveness and efficiency of the proposed MADE.

The remaining contents of this paper are partitioned into five sections. Section 2 briefly introduces no-wait FSSP and MNFSSP. Section 3 provides a brief review of DE. Section 4 presents MADE in detail, while Sect. 5 presents and discusses simulation results and comparisons. Finally,

Sect. 6 gives some conclusions and states future research directions.

## 2 NFSSP and MNFSSP

### 2.1 NFSSP

The no-wait FSSP with $n$ jobs and $m$ machines can be described as follows: given the processing time $p(i, j)$ of job $i$ on machine $j$, each of $n$ jobs will be sequentially processed on machine $1,2, \ldots, m$. At any time, each machine can process at most one job and each job can be processed on at most one machine. The sequence in which the jobs are to be processed is the same for each machine. To follow the no-wait restrictions, the difference between the completion time of the last operation of a job and the start time of its first operation is equal to the sum of the processing times of its operations. In other words, the operation of each job must be processed without interruptions between consecutive machines. The problem is to find a sequence or permutation for processing all jobs on all machines so that one or more given objectives are optimized. The objective widely used is the minimization of the maximum completion time, i.e., makespan $\left(C_{\text {max }}\right)$.

Let $\pi=\left\{\pi_{1}, \pi_{2}, \ldots, \pi_{n}\right\}$ denote the permutation of jobs to be processed, $P_{\text {sum }}\left(\pi_{j}\right)$ the total processing time of job $\pi_{j}$ on all machines, $M D\left(\pi_{j-1}, \pi_{j}\right)$ the minimum delay on the first machine between the start of job $\pi_{j}$ and $\pi_{j-1}$ restricted by the no-wait constraint. Then $M D$ can be calculated as follows:

$$
\begin{align*}
M D\left(\pi_{j-1}, \pi_{j}\right)= & p\left(\pi_{j-1}, 1\right) \\
& +\max \left[0, \max _{2 \leq k \leq m}\left\{\sum_{h=2}^{k} p\left(\pi_{j-1}, h\right)\right.\right. \\
& \left.\left.-\sum_{h=1}^{k-1} p\left(\pi_{j}, h\right)\right\}\right] . \tag{1}
\end{align*}
$$

Thus, the makespan can be defined as
$C_{\max }(\pi)=\sum_{j=2}^{n} M D\left(\pi_{j-1}, \pi_{j}\right)+P_{\text {sum }}\left(\pi_{n}\right)$.
where $P_{\text {sum }}\left(\pi_{n}\right)=\sum_{k=1}^{m} p\left(\pi_{n}, k\right)$.
The aim of the no-wait FSSP with the makespan criterion is to find a permutation $\pi^{*}$ in the set of all permutations $\Pi$ such that
$C_{\max }\left(\pi^{*}\right)=\min _{\pi \in \Pi} C_{\max }(\pi)$.
Figure 1 shows an example of a no-wait FSSP with $n=4$ and $m=4$.


Fig. 1 No-wait FSSP example with $n=4$ and $m=4$

### 2.2 MNFSSP

### 2.2.1 Objective functions

For a FSSP, let $C\left(\pi_{j}, k\right)$ denote the completion time of job $\pi_{j}$ on machine $k$. If there exists a due date $d_{j}$ for job $j$, we can define $L\left(\pi_{j}\right)=C\left(\pi_{j}, m\right)-d_{j}$ as the lateness of job $j$. Then, the tardiness and earliness of job $\pi_{j}$ can be defined as $T\left(\pi_{j}\right)=\max \left\{L\left(\pi_{j}\right), 0\right\}$ and $E\left(\pi_{j}\right)=\max \left\{-L\left(\pi_{j}\right), 0\right\}$, respectively. In some real application, machine idleness may be considered. Let $I_{k}(\pi)=C\left(\pi_{n}, k\right)-\sum_{j=1}^{n} p\left(\pi_{j}, k\right)$ denote the idleness time on machine $k$. Besides, we can use the indicator function $U\left(\pi_{j}\right)$ to denote whether job $\pi_{j}$ is $\operatorname{tardy}\left(U\left(\pi_{j}\right)=1\right)$ or not $\left(U\left(\pi_{j}\right)=0\right)$. Assuming $\lambda_{j}$ is a possible weight associated to job $j$, the following objective functions are frequently used (Pinedo 2002):
(1) Maximum completion time or makespan $C_{\max }(\pi)=$ $C\left(\pi_{n}, m\right)$;
(2) Total weighted completion time
$C_{w}(\pi)=\sum_{j=1}^{n} \lambda_{j} C\left(\pi_{j}, m\right) ;$
(3) Maximum tardiness $T_{\max }(\pi)=\max _{j} T\left(\pi_{j}\right)$;
(4) Total weighted tardiness $T_{w}(\pi)=\sum_{j=1}^{n} \lambda_{j} T\left(\pi_{j}\right)$;
(5) Total machine idleness $I_{\text {sum }}(\pi)=\sum_{k=1}^{m} I_{k}(\pi)$;
(6) Maximum earliness $E_{\max }(\pi)=\max _{j} E\left(\pi_{j}\right)$;
(7) Total weighted earliness $E_{w}=\sum_{j=1}^{n} \lambda_{j} E\left(\pi_{j}\right)$;
(8) Total number of tardy jobs $N_{T}(\pi)=\sum_{j=1}^{n} U\left(\pi_{j}\right)$; and so on.

### 2.2.2 MNFSSP

For the MNFSSP, some of objectives mentioned in Sect. 2.2.1 can be considered simultaneously. However, these objectives often conflict with themselves, that is, an improvement in one objective may worsen another. Since there is usually no such a solution that is the best to all objectives, the multi-objective optimization algorithms are required to find a set of optimal solutions (called non-dominated solutions) (Ishibuchi et al. 2003; Arroyo and Armentano 2005). Without loss of generality, a general multi-objective optimization problem (MOP)
with $w$ objectives can be described as follows:
$\operatorname{Minimize} f_{1}(\mathbf{x}), f_{2}(\mathbf{x}), \ldots, f_{w}(\mathbf{x})$
subject to $\mathbf{x} \in \mathbf{X}$,
where $f_{1}(\mathbf{x}), f_{2}(\mathbf{x}), \ldots, f_{w}(\mathbf{x})$ are $w$ objectives to be minimized, $\mathbf{x}$ is a vector of decision variables, and $\mathbf{X}$ is the set of feasible solution.

To multi-objective optimization, the following basic definitions are of importance:
(1) Pareto dominance: A solution $\mathbf{x}_{1}$ is said to (Pareto) dominate another solution $\mathbf{x}_{2}\left(\right.$ denoted $\left.\mathbf{x}_{\mathbf{1}} \succ \mathbf{x}_{\mathbf{2}}\right)$ if and only if

$$
\begin{align*}
& \left(\forall i \in\{1,2, \ldots, w\}: f_{i}\left(\mathbf{x}_{\mathbf{1}}\right)<f_{i}\left(\mathbf{x}_{\mathbf{2}}\right)\right) \\
& \quad \wedge\left(\exists j \in\{1,2, \ldots, w\}: f_{j}\left(\mathbf{x}_{\mathbf{1}}\right)<f_{j}\left(\mathbf{x}_{\mathbf{2}}\right)\right) . \tag{5}
\end{align*}
$$

(2) Optimal Pareto solution: A solution $\mathbf{x}_{1}$ is said to be an optimal Pareto solution if and only if there is no any solution $\mathbf{x}_{2}$ that satisfies $\mathbf{x}_{2} \succ \mathbf{x}_{1}$.
(3) Optimal Pareto set: The set containing all optimal Pareto solutions is said as optimal Pareto set.
(4) Optimal Pareto front: The set of all objective function values corresponding to the solutions in the optimal Pareto set is said as optimal Pareto front.

According to (Deb et al. 2002), basically two main goals should be considered to evaluate the obtained non-dominated solutions: (1) convergence to the optimal Pareto front; (2) maintenance of diversity (i.e., spread and distribution) of the obtained non-dominated solutions.

## 3 Introduction to differential evolution

DE is a class of population-based evolutionary algorithms, which absorbs the concepts of "population" from GA and "self-adapting mutation" from evolution strategy (ES). The procedure of DE is almost the same as that of GA whose main operations are mutation, crossover, and selection. The main difference between DE and GA lies in the mutation operation. In DE, it starts with the random initialization of a population of individuals in the search space and works on the cooperative behaviors of the individuals in the population. At each generation, the mutation and crossover operators are applied to individuals to generate a new population. Then, the one-to-one greedy selection takes place and the population is updated.

The basic scheme of DE, which is denoted as $D E /$ rand/l /bin, can be summarized as follow.

Let the $i$ th individual in the $N$-dimensional search space at generation $t$ be $X_{i}(t)=\left[x_{i, 1}, x_{i, 2}, \ldots, x_{i, N}\right]$
( $i=1,2, \ldots, P S$ ), where $P S$ denotes the size of the population, and $X_{i}(t)$ is a real vector.

Step 1: DE's initialization. Randomly initialize the population with $P S$ individuals and determine the best individual bestit with the best objective value.
Step 2: DE's mutation. In order to obtain each individual's corresponding mutant vector $V_{i}(t+1)=\left[v_{i, 1}\right.$ $\left.(t+1), \ldots, v_{i, N}(t+1)\right]$, mutation operation is performed for each individual according to the following equation:
$V_{i}(t+1)=X_{r 1}(t)+F *\left(X_{r 2}(t)-X_{r 3}(t)\right)$,
where $r 1, r 2, r 3 \in\{1,2, \ldots, P S\}$ are randomly chosen and mutually different and also different from the current index $i, F \in(0,2)$ is a constant called scaling factor which controls amplification of the differential variation $X_{r 2}(t)-X_{r 3}(t) . X_{r 1}(t)$ is the base vector to be perturbed.
Step 3: DE's crossover. To get each individual's trial vector $U_{i}(t+1)=\left[u_{i, 1}(t+1), \ldots, u_{i, N}(t+1)\right]$, crossover operation is performed between each individual and its corresponding mutant vector by the following equation:

$$
\begin{align*}
& u_{i, j}(t+1) \\
& = \begin{cases}v_{i, j}(t+1), & \text { if }(\operatorname{rand}(j)<C R) \text { or } \\
x_{i, j}(t), & j=\operatorname{randn}(i), \\
\text { otherwise } .\end{cases}  \tag{7}\\
& \quad j=1, \ldots, N,
\end{align*}
$$

where $\operatorname{rand}(j)$ is the $j$ th evaluation of a random number uniformly distributed in the range of [0,1], randn (i) is a randomly chosen index from the set $\{1,2, \ldots, N\}, C R \in[0,1]$ is a constant crossover parameter that controls the diversity of the population.
Step 4: DE's selection. To generate the new individual for the next generation, selection operation is performed between each individual and its corresponding trial vector by the following greedy selection criterion:

$$
\begin{align*}
& X_{i}(t+1) \\
& \quad= \begin{cases}U_{i}(t+1), & \text { if } f\left(U_{i}(t+1)\right)<f\left(X_{i}(t)\right), \\
X_{i}(t), & \text { otherwise } .\end{cases} \tag{8}
\end{align*}
$$

where $f$ is the objective function and $X_{i}(t+1)$ is the individual of the new population.

Step 5: Update bestit. If a stopping criterion is met, then output bestit and its objective value; otherwise go back to Step 2.

The key parameters in DE are the size of population $(P S)$, the scaling factor $(F)$, and the crossover parameter $(C R)$. Proper configuration of these parameters can increase the convergence velocity and robustness of the search process. In (Storn and Price 1997) some suggestions have been given for selecting suitable parameters for DE.

There are also some other DE variants (Price and Storn 2007), only differ in the type of mutation operation and crossover operation. The general format of DE is $D E / x / y / z$, where $x$ represents a base vector to be mutated/perturbed, $y$ is the number of difference vectors used for perturbation of $x$, and $z$ stands for the type of crossover being used (bin: binomial; exp: exponential).

## 4 MADE for MNFSSP

In this section, we will present the memetic DE for no-wait FSSP after explaining the solution representation, speedup computing method, DE-based search, problem-dependent local search and multi-objective handling techniques.

### 4.1 Solution representation

Due to the continuous nature of DE , the standard encoding scheme of DE cannot be directly adopted for FSSPs. So, it is crucial to develop a suitable mapping scheme that converts the individuals (continuous vectors) to the job sequence. In this paper, we design a largest-order-value (LOV) rule based on random key representation (Bean 1994) to convert individual $X_{i}=\left[x_{i, 1}, x_{i, 2}, \ldots, x_{i, n}\right]$ in DE to the job solution or permutation vector $\pi_{i}=\left[\pi_{i, 1}, \pi_{i, 2}, \ldots, \pi_{i, n}\right]$. Some other conversion techniques can be found in (Tasgetiren et al. 2004; Price et al. 2005). The conversion procedure is as follows:

Step 1: Rank all elements in $X_{i}=\left[x_{i, 1}, x_{i, 2}, \ldots, x_{i, n}\right]$ by descending order to obtain a sequence $\varphi_{i}=\left[\varphi_{i, 1}\right.$, $\left.\varphi_{i, 2}, \ldots, \varphi_{i, n}\right]$.
Step 2: Calculate the job permutation $\pi_{i}$ by the following formula:
$\pi_{i, \varphi_{i, l}}=l$,
where the dimension $l$ varies from 1 to $n$.
To better understand the LOV rule, a simple example ( $n=6$ ) is illustrated in Table 1, where the individual is $X_{i}=[1.36,3.85,2.55,0.63,2.68,0.82]$. The details that correspond with the steps of the conversion procedure are given as follows:

Table 1 Solution representation

| Dimension $l$ | 1 | 2 | 3 | 4 | 5 | 6 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $x_{i, l}$ | 1.36 | 3.85 | 2.55 | 0.63 | 2.68 | 0.82 |
| $\varphi_{i, l}$ | 4 | 1 | 3 | 6 | 2 | 5 |
| $\pi_{i, l}$ | 2 | 5 | 3 | 1 | 6 | 4 |

Step 1: Since $x_{i, 2}$ is the largest value of $X_{i}, x_{i, 2}$ is selected first and assigned the rank value 1 . Then $x_{i, 5}$ is selected second and assigned the rank value 2 . In the same way, $x_{i, 3}, x_{i, 1}, x_{i, 6}$ and $x_{i, 4}$ are assigned the rank values $3,4,5$, and 6 , respectively. Thus, the sequence is $\varphi_{i}=[4,1,3,6,2,5]$.
Step 2: According to (9), if $l=1$, then $\varphi_{i, 1}=4$ and $\pi_{i, \varphi_{i, 1}}=\pi_{i, 4}=1$; if $l=2$, then $\varphi_{i, 2}=1$ and $\pi_{i, \varphi_{i, 2}}=\pi_{i, 1}=2$; if $l=3$, then $\varphi_{i, 3}=3$ and $\pi_{i, \varphi_{i, 3}}=\pi_{i, 3}=3$; and so on. Thus, we obtain the job permutation $\pi_{i}=[2,5,3,1,6,4]$.

Obviously, such a conversion process is very simple, and it makes DE suitable for solving FSSPs.

In our MADE, memes or local searchers are not directly applied to individual $X_{i}(t)$ with real values, but to the job permutation $\pi_{i}$. Thus, after the whole local search completes, $X_{i}(t)$ should be repaired because its corresponding job permutation should match the permutation resulted by the local search. Based on the mechanism of LOV rule, the repair process is easy to implement, which is given as follows:

Step 1: Calculate the sequence $\varphi_{i}$ by the following formula:

$$
\begin{equation*}
\varphi_{i, \pi_{i, l}}=l . \tag{10}
\end{equation*}
$$

where $l$ varies from 1 to $n$.
Step 2: Values in $X_{i}(t)$ are rearranged to keep consistent with $\varphi_{i}$. That is, $X_{i, l}$ should be set to the $\varphi_{i, l}$ th largest value of the old $X_{i}(t)$.

A simple instance on the repair is shown in Tables 2 and 3 , where $\pi_{i, 3}=3$ and $\pi_{i, 4}=1$ are interchanged. As seen in Table 2, the LOV rule is violated because the new job permutation $\pi_{i}$ does not match the old individual $X_{i}(t)$. Thus, $X_{i}(t)$ and $\varphi_{i}$ should be repaired, as the results in Table 3. The details that match with the steps of the repair process are given as follows:

Table 2 Job solution resulted by local search (before repairing)

| Dimension $l$ | 1 | 2 | 3 | 4 | 5 | 6 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $x_{i, l}$ | 1.36 | 3.85 | 2.55 | 0.63 | 2.68 | 0.82 |
| $\varphi_{i, l}$ | 4 | 1 | 3 | 6 | 2 | 5 |
| $\pi_{i, l}$ | 2 | 5 | $\underline{\mathbf{1}}$ | $\underline{\mathbf{3}}$ | 6 | 4 |

Table 3 Job solution resulted by local search (after repairing)

| Dimension $l$ | 1 | 2 | 3 | 4 | 5 | 6 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $x_{i, l}$ | $\underline{\mathbf{2 . 5 5}}$ | 3.85 | $\underline{\mathbf{1 . 3 6}}$ | 0.63 | 2.68 | 0.82 |
| $\varphi_{i, l}$ | $\underline{\mathbf{3}}$ | 1 | $\underline{\mathbf{4}}$ | 6 | 2 | 5 |
| $\pi_{i, l}$ | 2 | 5 | $\underline{\mathbf{1}}$ | $\underline{\mathbf{3}}$ | 6 | 4 |

Step 1: Rearrange $\varphi_{i}$ by equation (10). That is, if $l=1$, then $\pi_{i, 1}=2$ and $\varphi_{i, \pi_{i, 1}}=\varphi_{i, 2}=1$; if $l=2$, then $\pi_{i, 2}=5$ and $\varphi_{i, \pi_{i, 2}}=\varphi_{i, 5}=2$; and so on. Then we can get the new sequence $\varphi_{i}=[3,1,4,6,2,5]$ in Table 3.
Step 2: Rearrange $X_{i}(t)$ to keep consistent with the new $\varphi_{i}$. If $l=1$, then $\varphi_{i, 1}=3$. That is to say, $X_{i, 1}$ should be set to the third largest value of the old $X_{i}(t)$ (i.e., 2.55). If $l=2$, then $\varphi_{i, 2}=1$ and $X_{i, 2}$ should be set to the largest value of the old $X_{i}(t)$ (i.e., 3.85). Similarly, the new individual $X_{i}(t)=$ [2.55, 3.85, 1.36, 0.63, 2.68, 0.82] can be obtained in Table 3.

### 4.2 Speed-up computing method

In FSSPs, $M D\left(\pi_{j-1}, \pi_{j}\right)$ is not only determined by the job $\pi_{j-1}$ and $\pi_{j}$ but also affected by the jobs before $\pi_{j-1}$. But in no-wait FSSPs (NFSSPs), $M D\left(\pi_{j-1}, \pi_{j}\right)$ is only decided by the job $\pi_{j-1}$ and $\pi_{j}$. Based on this property of NFSSPs, one method can be adopted to reduce the computing complexities of the objective functions in Section 2.2. That is, $M D\left(\pi_{j-1}, \pi_{j}\right)$ and $P_{\text {sum }}\left(\pi_{j}\right)$ can be calculated and saved in the initial phase of MADE and then can be used as constant values in the evolution phase of MADE.

According to equation (1), $M D\left(\pi_{j-1}, \pi_{j}\right)$ can be calculated by the algorithm in Appendix 1. This algorithm has a computing complexity $(\mathrm{CC})$ of $O(\mathrm{~m})$. In the initial phase of MADE, $M D\left(\pi_{j-1}, \pi_{j}\right)$ and $P_{\text {sum }}\left(\pi_{j}\right)\left(\pi_{j-1}, \pi_{j} \in\right.$ $\{1, \ldots, n\})$ need to be calculated $n(n-1)$ times and $n$ times respectively. Since $n$ is usually much larger than $m$, the total CC of $M D\left(\pi_{j-1}, \pi_{j}\right)$ and $P_{\text {sum }}\left(\pi_{j}\right)\left(\pi_{j-1}, \pi_{j} \in\{1, \ldots, n\}\right)$ is $O\left(n^{2} m\right)$.

For the sake of simplicity, let MADE_nospeedup denote MADE without speed-up method, TCC_MADE_nospeedup (a certain objective function) denote the total CC of calculating a certain objective function in MADE_nospeedup and TCC_MADE( a certain objective function) denote the total CC of calculating a certain objective function in MADE. Suppose the total solution evaluation times (TET) of any objective function in MADE_nospeedup and MADE are $K$.

### 4.2.1 Analysis of the $C C$ of calculating $C_{\max }(\pi)$

In MADE_nospeedup, it can be seen from Eq. (2) that the CC of $C_{\max }(\pi)$ is $O(n m)$. Then, TCC_MADE_nospeedup
$\left(C_{\max }(\pi)\right)$ is $O(K n m)$. In MADE, $L\left(\pi_{j-1}, \pi_{j}\right)$ and $P_{\text {sum }}\left(\pi_{j}\right)$ can be regarded as constant values in the evolution phase. Then, the CC of $C_{\max }$ is reduced to $O(n)$. Thus TCC_MADE $\left(C_{\max }(\pi)\right)$ is $O\left(n^{2} m+K n\right)$. Because $K$ is usually much larger than $n m$, TCC_MADE $\left(C_{\max }(\pi)\right)$ is reduced from $O(K n m)$ of TCC_MADE_nospeedup $\left(C_{\max }(\pi)\right)$ to $O(K n)$.

### 4.2.2 Analysis of the CC of calculating $I_{\text {sum }}(\pi)$

The total machine idleness $I_{\text {sum }}(\pi)$ can be defined as follow:

$$
\begin{align*}
I_{\text {sum }}(\pi)= & \sum_{k=1}^{m} I_{k}(\pi)=m \sum_{x=2}^{n} M D\left(\pi_{x-1}, \pi_{x}\right) \\
& +\sum_{k=1}^{m} \sum_{y=1}^{k} p\left(\pi_{n}, y\right)-\sum_{k=1}^{m} \sum_{j=1}^{n} p\left(\pi_{j}, k\right) \\
= & m \sum_{x=2}^{n} M D\left(\pi_{x-1}, \pi_{x}\right)+\sum_{k=1}^{m} \sum_{y=1}^{k} p\left(\pi_{n}, y\right) \\
& -\sum_{j=1}^{n} P_{\text {sum }}\left(\pi_{j}\right) . \tag{11}
\end{align*}
$$

where $\sum_{k=1}^{m} \sum_{y=1}^{k} p\left(\pi_{n}, y\right)$ can be computed in $O(m)$ by the algorithm in Appendix 2.

InMADE_nospeedup, the CCs of $m \sum_{x=2}^{n} M D\left(\pi_{x-1}, \pi_{x}\right)$ and $\sum_{k=1}^{m} \sum_{y=1}^{k} p\left(\pi_{n}, y\right)$ and $\sum_{j=1}^{n} P_{\text {sum }}\left(\pi_{j}\right)$ are $O(n m)$ and $O(\mathrm{~m})$ and $O(n m)$ respectively. And $n$ is larger than $m$. So, the CC of $I_{\text {sum }}(\pi)$ in MADE_nospeedup is $O(n m)$. In MADE, the CCs of $m \sum_{x=2}^{n} M D\left(\pi_{x-1}, \pi_{x}\right)$ and $\sum_{k=1}^{m}$ $\sum_{y=1}^{k} p\left(\pi_{n}, y\right)$ and $\sum_{j=1}^{n} P_{\text {sum }}\left(\pi_{j}\right)$ are $O(n)$ and $O(m)$ and $O(n)$ respectively. That is, the CC of $I_{\text {sum }}(\pi)$ in MADE is $O(n)$. Like the analysis in Sect. 4.2.1, TCC_MADE $\left(I_{\text {sum }}(\pi)\right)$ is decreased from $O(\mathrm{Knm})$ of TCC_MADE_nospeedup $\left(I_{\text {sum }}(\pi)\right)$ to $O(K n)$.

### 4.2.3 Analysis of the CCs of calculating other objective functions in Sect. 2.2

Let $O F$ denote any objective function in Section 2.2 except $C_{\max }(\pi)$ and $I_{\text {sum }}(\pi)$. When calculating $O F, C\left(\pi_{j}, m\right)\left(\pi_{j} \in\right.$ $\{1, \ldots, n\})$ is required to be computed first, which can be obtained by the algorithm in Appendix 3. The CC of this algorithm is $O(\mathrm{~nm})$, which can be decreased from $O(\mathrm{~nm})$ to $O(n)$ by using the speed-up method. Obviously, the CC of computing $O F$ is equal to that of computing $C\left(\pi_{j}, m\right)\left(\pi_{j} \in\right.$ $\{1, \ldots, n\})$. This means TCC_MADE $(O F)$ can be decreased from $O(\mathrm{Knm})$ of TCC_MADE_nospeedup $(O F)$ to $O(K n)$.

### 4.3 DE-based search

In MADE, DE-based search is designed based on $D E /$ rand-to-best/l/exp scheme to perform parallel exploration, in which "exp" of "DE/rand-to-best/l/exp" means the exponential crossover is adopted and "rand-to-best" means the base vector is the best individual of the current population (Price and Storn 2007). Thus, those individuals performing DE-based operation will share the information of the best individual of the population. Note that, DE-based evolution is not performed on permutation-based solution space but continuous space. So, DE is used to stress exploration in a continuous searching space. Furthermore, DE-based search can be regarded as a kind of scatter search. In the mutation and crossover phase, each individual can transform probabilistically to any other individual in the solution space. Therefore, a wide range of solution space can be searched. In the selection phase, only the better individual can be accepted. This means that the DE-based search has the ability to reach enough promising regions over the solution space.

Because of the parallel evolutionary framework of DE, it is easy to incorporate local search into DE to design effective memetic algorithms. Next, we will present the problemdependent local search.

### 4.4 Problem-dependent Local Search

For the MNFSSPs, we designed local searchers or memes based on the following three neighborhoods which are often employed in the literature. (i) Remove the job at the $u$ th dimension and insert it in the $v$ th dimension of the job solution $\pi(\operatorname{insert}(\pi, u, v))$, (ii) interchange the job at the $u$ th dimension and the job at the $v$ th dimension of the job solution $\pi$ (interchange $(\pi, u, v)$ ), (iii) swap the two neighboring jobs at the dimension $u$ and $(u+1)$ of the job solution $\pi(\operatorname{swap}(\pi, u, u+1))$.

According to (Schiavinotto and Stützle 2007), the diameter of Insert is $n-1$. That is, using Insert at most $n-1$ times, one solution $\pi$ can transit to any other solution. The diameters of Interchange and Swap are $n-1$ and $n(n-1) / 2$, respectively. Therefore, the solutions in the big valley caused by Insert or Interchange are closer to each other than those in the big valley caused by Swap. This means Insert and Interchange can perform a more efficient and thorough search than Swap with the same computational efforts. So we select one neighborhood $N_{\text {exploitation }}$ from Insert and Interchange to perform exploitation in local search. However, it is easy to fall into local optima only with a single neighborhood. Inspired by the observation that a local optimum within one neighborhood is not necessary one within another neighborhood (Mladenovic and Hansen 1997), we choose a neighborhood $N_{\text {perturbation, }}$ which is different from
$N_{\text {exploitation }}$, to execute a perturbation operation before perform exploitation.

As for MNFSSPs, different objectives, which are usually conflicting or not positively correlated, cause different shapes of big valleys. Thus, it is very difficult for a solution to simultaneously reach the bottoms of all big valleys. This indicates that only one type of meme is unlikely to efficiently exploit the solution space. Geiger (2007) also showed that not a single neighborhood performs best for all multi-objective FSSPs and combining different neighborhoods in a random fashion can significantly improve the solutions quality. In addition, Neri et al. (2007) presented an adaptive multimeme algorithm for designing multidrug therapies, which utilized different memes to exploit the solution space from complementary perspectives and can obtain very satisfactory solution. Therefore, we design three types of meme to enrich the search behavior and enhance the search ability. These memes are Meme(Interchange, Insert, LS_Len), Meme(Insert, Interchange, LS_Len) and Meme(Swap, Insert, LS_Len), in which $L S_{-}$Len denotes the exploitation depth of a meme. The general form of these memes, namely Meme ( $N_{\text {perturbation }}, N_{\text {exploitation }}, L S \_L e n$ ), is given as follows:

Step 1: Convert individual $X_{i}(t)$ to a job permutation $\pi_{i}{ }^{0}$ according to the LOV rule.
Step 2: Perturbation phase.
Randomly select $u$ and $v$, where $u \neq v$;
$\pi_{i}=N_{\text {pertubation }}\left(\pi_{i_{-} 0}, u, v\right) ; / / \quad N_{\text {perturbation }}$
Step 3: Exploitation phase.
Set kcount $=1$;
Do
Randomly select $u$ and $v$, where $u \neq v$;
$\pi_{i_{-} 1}=N_{\text {exploitation }}\left(\pi_{i}, u, v\right) ; \quad / / \quad N_{\text {exploitation }}$
if $f\left(\pi_{i_{-} 1}\right)$ dominates $f\left(\pi_{i}\right)$, then $\pi_{i}=\pi_{i_{-} 1}$;
kcount $=$ kcount +1 ;
While kcount $<L S \_$Len
Step 4: If $f\left(\pi_{i}\right)$ dominates $f\left(\pi_{i_{-}} 0\right)$, then $\pi_{i_{-} 0}=\pi_{i}$.
Step 5: Convert $\pi_{i \_0}$ back to $X_{i}(t)$.
The characteristic of the above algorithm lies in two aspects. (1) In Step 2, $u$ and $v$ performing perturbation are randomly chosen and the new solution is always accepted, so the meme can avoid falling into local optima and also can reach different regions. (2) In Step 3, the new solution $\pi_{i_{-} 1}$ is accepted only if it dominates the old solution $\pi_{i}$. Thus, the meme can guide the search to the promising regions nearby the bottoms of different valleys in a relatively short time and
spend more time to perform $N_{\text {exploitation }}$-based thorough search in these regions.
If $N_{\text {pertubation }}=$ Interchange and $N_{\exp \text { loitation }}=$ Insert, $\operatorname{Meme}\left(N_{\text {perturbation }}\right.$, $\left.N_{\text {exploitation }}, L S \_L e n\right)$ is transformed to Meme(Interchange, Insert, LS_Len). Similarly, the other two memes can also be obtained.

### 4.5 Multi-objective handling techniques

In order to handle multi-objective no-wait FSSPs (MNFSSPs), several techniques are adopted as follows.
(1) For any big valley of MNFSSPs, the optimal Pareto solutions and good solutions lie not only in the bottom part but also in the sub-regions near the bottom part. Therefore, in order to exploit enough sub-regions to find all optimal Pareto solutions, both global search and local search should be stressed and balanced. In the former (Qian et al. 2009), we investigated how to reasonably fuse DE-based global search and problembased local search for solving multi-objective FSSPs with limited buffers and found that applying local search to $1 / 4-1 / 5$ individuals in population can achieve better results. Based on our experiments, similar conclusion can also be drawn for MNFSSPs. In MADE, $1 / 5$ individuals are selected to apply local search.
(2) In MADE, a tentative non-dominated solutions set $S$ is used to store the obtained non-dominated job permutations and the corresponding individuals. This elitism can improve the optimization speed of multi-objective GA (Zitzler et al. 2000). According to (Jonathan et al. 2003), restricting the number of solutions in $S$ can induce retreating and shrinking estimated Pareto fronts. Fortunately, the number of solutions in $S$ is usually less than 30 . Thus, it is not necessary to define an upper bound for $S$. At every generation, $S$ is updated by the new population. In particular, if a solution in the new population is dominated by any solution in $S$, it will be discard; otherwise, it will be added to $S$, and all the solutions dominated by the added one are deleted from $S$.
(3) To enrich the searching direction and to speed up the total convergence process, in MADE all non-dominated solutions in $S$ are treated equally, and one solution randomly selected from $S$ is used as the best individual bestit (base vector) of the current population.
(4) To obtain non-dominated solutions with reasonable diversity and good proximity, two measures, whose effectiveness has been validated in (Qian et al. 2009), are adopted at the DE's selection step in MADE. The first one is that the trail vector is compared with the individual $r 1$ rather than individual $i$. The second one
is that the dominated solution can be accepted with a small probability.

### 4.6 Procedure of MADE

Based on the above solution conversion, speed-up computing method, DE-based search, problem-dependent local search, solution repair mechanism and multi-objective handling techniques, the procedure of MADE is proposed as follows:

Based on the above sub-sections, the procedure of MADE is given as follows:

Step 0: Let $G$ denote a generation, $\operatorname{Pop}(t)$ a population with size $P S$ in generation $t, X_{i}(t)$ the $i$ th individual with dimension $N(N=n)$ in $\operatorname{Pop}(t), x_{i, j}(t)$ the $j$ th variable of individual $X_{i}(t), t m p_{j}$ the $j$ th variable of tmp,CR the crossover probability, and random $(0,1)$ the random value in the interval $[0,1]$. The values of the objectives of each individual are calculated by speed-up method.
Step 1: Calculate and save $M D\left(\pi_{i}, \pi_{j}\right)$ and $P_{s u m}\left(\pi_{j}\right)\left(\pi_{i}\right.$, $\left.\pi_{j} \in\{1, \ldots, n\}\right)$.
Step 2: Input $N, P S, C R \in[0,1]$. Set $S=\phi$, and let initial bounds be lower $\left(x_{i, j}\right)=0, \operatorname{upper}\left(x_{i, j}\right)=4$, $j=1, \ldots, N$. As for $D E /$ rand-to-best/l/exp scheme, the mutation needs to randomly choose different $r 1, r 2$ and index $i$ from $\{1,2, \ldots, P S\}$. So $P S$ must be greater or equal to 3 .
Step 3: Population initialization.
Generate $x_{i, j}(0)=\operatorname{lower}\left(x_{i, j}\right)+\operatorname{random}(0,1) *$ $\left(\operatorname{upper}\left(x_{i, j}\right)-\operatorname{lower}\left(x_{i, j}\right)\right), j=1, \ldots, N$ for $i=1, \ldots, P S$.
Step 4: Update $S$ and let $t=1$.
Step 5: Evolution phase (between Step 5 and Step 12). Let $i=1$.
Step 6: Set the trial vector tmp $=X_{i}(t-1)$ and $L=0$. Randomly select an individual from $S$ as bestit, randomly select $j \in(1, \ldots, N)$, and randomly select $r 1, r 2 \in(1, \ldots, P S)$, where $r 1 \neq r 2 \neq i$.
Step 7: Perform DE's mutation and crossover.
Step 7.1: Let $t m p_{j}=t m p_{j}+F *\left(\right.$ bestit $_{j}-$ tmp $\left._{j}\right)+$ $F *\left(x_{r 1, j}(t-1)-x_{r 2, j}(t-1)\right)$.

If $\operatorname{tmp}_{j}<\operatorname{lower}\left(x_{i, j}\right)$, then let $\operatorname{tmp} p_{j}=$ $2 * \operatorname{lower}\left(x_{i, j}\right)-\operatorname{tmp}_{j}$.
If $\operatorname{tmp}_{j}>\operatorname{upper}\left(x_{i, j}\right)$, then let $t m p_{j}=$ $2 * \operatorname{upper}\left(x_{i, j}\right)-t m p_{j}$.

Step 7.2: Set $j=(j+1) \bmod N$ and $L=L+1$.
Step 7.3: If $j=0$, then $j=N$.
Step 7.4: If $($ random $(0,1)<C R)$ and $(L<N)$, then go to Step 7.1.

Step 8: Perform DE's selection.


Fig. 2 The framework of the MADE

If $\left(\left(\operatorname{tmp} p\right.\right.$ dominates $\left.X_{r 1}(t-1)\right)$ or $($ random $(0,1)<$ $0.05)$ ), then let $X_{i}(t)=t m p$; else, let $X_{i}(t)=$ $X_{i}(t-1)$.
Step 9: If $(i \bmod 5)=1$, then
Randomly select $L S \in(1,2,3)$;
If $L S=1$ then apply Meme(Interchange, Insert, $L S \_$Len ) to $X_{i}(t)$;
If $L S=2$ then apply Meme(Insert, Interchange, $L S_{-}$Len) to $X_{i}(t)$;
If $L S=3$ then apply Meme(Swap, Insert, $L S_{-}$Len) to $X_{i}(t)$;
Step 10: Let $i=i+1$. If $i<P S$, then go to Step 6.
Step 11: Update $S$.
Step 12: Let $t=t+1$. If $t<t \_m a x$, then go to Step 5.
Step 13: Output $S$.
To be more straightforward, a MADE framework is illustrated in Fig. 2. It can be seen that DE and memes are hybridized. On one aspect, the inherent random and scatter search mechanism of DE and special designed DE's selection are utilized to find enough promising sub-regions over the whole solution space. On the other aspect, three problem-specific memes are applied to perform thorough exploitation in
certain sub-regions. Due to the reasonable fusion of DE and memes, searching behavior can be enriched, and global exploration and local exploitation are stressed and well balanced.

## 5 Simulation results and comparisons

### 5.1 Experimental setup

To test the performances of the proposed MADE for MNFSSPs, numerical simulations are carried out with 28 well-studied benchmarks (i.e., Car1, Car5, Car8, Rec01, Rec05, Rec09, Rec11, Rec15, Rec19, Rec21, Rec25, Rec29, Rec31, Rec35, Rec39, Ta061, Ta065, Hel1, Ta071, Ta075, Ta081, Ta085, Ta091, Ta095, Ta101, Ta105, Ta111, Ta115) with different scales (Carlier 1978; Reeves 1995; Taillard; Heller 1960). In proposed MADE, parameters are set as follows: the population size $P S=60$, the scaling factor $F=$ 0.7 , the crossover parameter $C R=0.1$, the meme's exploitation depth $L S_{-} L e n=12 n$ when $n<75, L S \_$Len $=$ $n^{2} / 6$ when $n=100, L S \_L e n=n^{2} / 15$ when $n=200$, $L S_{-}$Len $=n^{2} / 30$ when $n=500$.

To analyze the effectiveness of MADE, two variants of MADE are compared, whose abbreviations are as follows:
(1): MADE_nospeedup: MADE without speed-up method.
(2): MADE_noSL: MADE without speed-up method and local searchers (i.e., memes).

Moreover, a famous multi-objective optimization algorithm, namely IMMOGLS2 (Ishibuchi et al. 2003), is also adopted for comparison. In IMMOGLS2, the population size is also set as $P S=60$, and other parameters are set the same as those in (Ishibuchi et al. 2003). That is, crossover probability $=0.9$, mutation probability $=0.6$, number of elite solutions $\left(N_{\text {elite }}\right)=10$, number of neighbors to be examined $(k)=2$, tournament size $=5$, and local search probability $\left(p_{L S}\right)=0.8$.

All algorithms are coded in Delphi 6.0 and experiments are executed on the same PC with Pentium IV 3.0 GHz CPU and 1 GB memory. Each benchmark is independently run 10 times with every algorithm for comparison.

In Sects. 5.3 and 5.4, makespan $C_{\max }(\pi)$ and maximum tardiness $T_{\max }(\pi)$ are considered as criteria. We set the two objectives as follows:
$\operatorname{Minimize} f_{1}(\pi)=C_{\max }(\pi)$ and $f_{2}(\pi)=T_{\max }(\pi)$,
where $\pi$ is a job permutation.
In the real application, the total machine idleness $I_{\text {sum }}$ sometimes plays a key role and has to be regarded as unutilized resources (Geiger 2007), and the total number of tardy jobs $N_{T}(\pi)$ is often monitored and relative to which managers are measured (Pinedo 2002). In order to examine the performance of MADE under these criteria, $I_{\text {sum }}(\pi)$ and total
$N_{T}(\pi)$ are also used as criteria. Because IMMOGLS2 adopts a scalar fitness function with random weights to handle multiobjectives and the value of $N_{T}(\pi)$ is much smaller $I_{\text {sum }}(\pi)$, we set the two objectives as follows:

Minimize $f_{1}(\pi)=I_{\text {sum }}(\pi)$ and $f_{2}(\pi)=1000^{*} N_{T}(\pi),(13)$
where constant multipliers are used in equation (13) to handle the two criteria.

Since MADE uses the concept of Pareto dominance to deal with multiple objectives, the performance of MADE is independent from constant multipliers. During the search process, both MADE and IMMOGLS2 use the above constant multipliers. But when evaluating the obtained non-dominated solutions by the performance metrics in Sect. 5.2, we set all constant multipliers as 1 .

The due date of each job is specified as follows:
(1) For each problem $p$, randomly generate a permutation $\pi^{r}$ of the jobs.
(2) Calculate the completion time of each job in the permutation $\pi^{r}$.
(3) Specify the due data of each job by
$d_{p, j}=c_{p, j}+\operatorname{random}\left[-C_{p}\left(\pi^{r}\right) / 50, C_{p}\left(\pi^{r}\right) / 50\right]$,
where $d_{p, j}$ is the due date of job $j$ to problem $p, c_{p, j}$ is the completion time of job $\pi_{j}^{r}$ to problem $p, C_{p}\left(\pi^{r}\right)$ is the makespan of $\pi^{r}$ to problem $p$, and random $\left[-C_{p}\left(\pi^{r}\right) / 50\right.$, $\left.C_{p}\left(\pi^{r}\right) / 50\right]$ is a random value in the interval $\left[-C_{p}\left(\pi^{r}\right) / 50\right.$, $\left.C_{p}\left(\pi^{r}\right) / 50\right]$.

### 5.2 Performance metrics

Unlike single-objective problems, proper comparison of two multi-objective algorithms itself is a multi-objective problem. That is, the two goals mentioned in Sect. 2.2.2 should be considered. Here, four performance metrics are used to evaluate the searching quality of the algorithm.
(1) Ratio of non-dominated solution ( $R N D S$ )

Let $S$ denote the union of the $K$ non-dominated solution sets (i.e., $S=S_{1} \cup \cdots \cup S_{K}$ ). A straightforward performance metric (Ishibuchi et al. 2003) of the non-dominated solution set $S_{j}$ with respect to the $K$ non-dominated solution sets is the ratio of solutions in $S_{j}$ that are not dominated by any other solutions in $S$. This metric is written as:

$$
\begin{equation*}
R N D S\left(S_{j}\right)=\frac{\left|S_{j}-\left\{\mathbf{x} \in S_{j} \mid \exists \mathbf{y} \in S: \mathbf{y} \succ \mathbf{x}\right\}\right|}{\left|S_{j}\right|} \tag{15}
\end{equation*}
$$

where $y \prec x$ means that the solution $x$ is dominated by the solution $y$. In the numerator of (15), dominated

Table 4 Comparisons of MADE_noSL with IMMOGLS2 when considering $f=\left(C_{\max }, T_{\max }\right)$ (same running time)

| Problem | $n, m$ | Tavg | MADE_noSL |  |  |  | IMMOGLS2 |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | ONVG | ONSN | $D I_{R}$ | AQ | ONVG | ONSN | $D I_{R}$ | AQ |
| Car1 | 11,5 | 2.201 | 7.800 | 7.000 | 4.894 | 4221.411 | 9.500 | 9.200 | 1.994 | 4202.432 |
| Car5 | 10,6 | 2.005 | 8.400 | 6.900 | 4.634 | 4883.763 | 9.000 | 9.000 | 0.050 | 4830.118 |
| Car8 | 8,8 | 1.532 | 6.000 | 6.000 | 10.587 | 4782.080 | 6.900 | 6.900 | 0.473 | 4761.811 |
| Rec01 | 20,5 | 4.925 | 9.300 | 2.500 | 25.769 | 859.575 | 9.300 | 9.100 | 8.126 | 807.743 |
| Rec05 | 20,5 | 5.130 | 9.400 | 3.000 | 22.483 | 830.390 | 12.700 | 12.400 | 5.497 | 794.026 |
| Rec09 | 20,10 | 6.181 | 8.200 | 1.800 | 32.450 | 1179.760 | 12.600 | 12.400 | 4.897 | 1091.125 |
| Rec11 | 20,10 | 6.386 | 7.400 | 1.300 | 38.893 | 1043.839 | 9.400 | 9.300 | 6.704 | 966.840 |
| Rec15 | 20,15 | 7.046 | 10.400 | 0.900 | 30.217 | 1397.505 | 12.600 | 12.500 | 2.940 | 1306.010 |
| Rec19 | 30,10 | 10.984 | 8.800 | 0.900 | 50.721 | 1812.499 | 12.400 | 12.400 | 4.867 | 1608.427 |
| Rec21 | 30,10 | 10.974 | 9.100 | 0.600 | 65.397 | 1795.125 | 10.900 | 10.900 | 3.270 | 1542.850 |
| Rec25 | 30,15 | 13.400 | 8.900 | 0.700 | 57.744 | 2205.373 | 8.400 | 8.400 | 8.539 | 1952.038 |
| Rec29 | 30,15 | 13.373 | 7.900 | 1.900 | 58.365 | 2095.286 | 11.700 | 11.700 | 9.005 | 1805.912 |
| Rec31 | 50,10 | 26.791 | 9.000 | 0.000 | 87.161 | 3169.323 | 10.000 | 10.000 | 0.000 | 2483.894 |
| Rec35 | 50,10 | 26.622 | 9.300 | 0.100 | 85.648 | 3337.035 | 16.100 | 16.100 | 0.209 | 2600.327 |
| Rec39 | 75,20 | 82.537 | 8.400 | 0.000 | 97.130 | 6841.359 | 16.500 | 16.500 | 0.000 | 5003.819 |
| Ta061 | 100,5 | 93.945 | 10.700 | 0.000 | 101.894 | 5339.674 | 15.200 | 15.200 | 0.000 | 3956.172 |
| Ta065 | 100,5 | 93.514 | 9.500 | 0.000 | 103.903 | 5305.148 | 13.300 | 13.300 | 0.000 | 3816.982 |
| Hel1 | 100,10 | 138.139 | 8.500 | 0.000 | 107.285 | 624.380 | 7.400 | 7.400 | 0.000 | 427.535 |
| Ta071 | 100,10 | 133.516 | 11.000 | 0.000 | 99.681 | 7065.041 | 19.400 | 19.400 | 0.000 | 5005.006 |
| Ta075 | 100,10 | 133.952 | 10.600 | 0.000 | 103.521 | 7047.056 | 17.400 | 17.400 | 0.000 | 4880.311 |
| Ta081 | 100,20 | 201.217 | 10.200 | 0.000 | 103.130 | 9512.533 | 18.400 | 18.400 | 0.000 | 6483.817 |
| Ta085 | 100,20 | 202.622 | 10.900 | 0.000 | 98.762 | 9174.423 | 20.300 | 20.300 | 0.000 | 6312.293 |
| Ta091 | 200,10 | 437.112 | 12.100 | 0.000 | 112.416 | 15435.132 | 15.000 | 15.000 | 0.000 | 9998.205 |
| Ta095 | 200,10 | 436.875 | 7.300 | 0.000 | 115.981 | 15615.812 | 12.300 | 12.300 | 0.000 | 9879.640 |
| Ta101 | 200,20 | 658.878 | 8.800 | 0.000 | 116.670 | 20047.310 | 16.500 | 16.500 | 0.000 | 12768.669 |
| Ta105 | 200,20 | 657.628 | 8.600 | 0.000 | 118.055 | 20647.405 | 17.500 | 17.500 | 0.000 | 12654.251 |
| Ta111 | 500,20 | 5156.385 | 9.100 | 0.000 | 128.427 | 56798.486 | 10.100 | 10.100 | 0.000 | 31407.120 |
| Ta115 | 500,20 | 5172.271 | 12.700 | 0.000 | 126.851 | 57069.386 | 14.200 | 14.200 | 0.000 | 33055.223 |
| Average |  |  | 9.225 | 1.200 | 75.310 | 9647.718 | 13.036 | 12.993 | 2.020 | 6300.093 |

solutions $x$ by other solutions $y$ in $S$ are removed from $S_{j} .\left|S_{j}\right|$ is the number of solutions in $S_{j} \cdot R N D S\left(S_{j}\right)=1$ means that all solutions in $S_{j}$ are not dominated by any solutions in $S$. On the contrary, $R N D S\left(S_{j}\right)=0$ represents that each solution in $S_{j}$ is dominated by some solutions in $S$. The higher the ratio $R N D S\left(S_{j}\right)$ is, the better the solution set $S_{j}$ is.
(2) Overall non-dominated vector generation (ONVG)

For an obtained non-dominated solution set $S_{j}$, the metric $O N V G$ is defined as $\left|S_{j}\right|$, which is the number of distinct non-dominated solutions.
(3) Overall non-dominated solutions number (ONSN) The metric ONSN is the number of those solutions in $S_{j}$ not dominated by any other solutions in $S$ :
$\operatorname{ONSN}\left(S_{j}\right)=\left|S_{j}-\left\{\mathbf{x} \in S_{j} \mid \exists \mathbf{y} \in S: \mathbf{y} \succ \mathbf{x}\right\}\right|$.

The larger the value of $\operatorname{ONSN}\left(S_{j}\right)$ is, the better the solution set $S_{j}$ is.
(4) Average distance $\left(D I_{R}\right)$

Let $d_{\mathbf{y x}}\left(S_{j}\right)$ denote the shortest normalized distance from a reference solution y to a solution set $S_{j}$, which is given as follows:

$$
\begin{equation*}
d_{\mathbf{y x}}\left(S_{j}\right)=\min _{\mathbf{x} \in S_{j}}\left\{\sqrt{\sum_{i=1}^{w}\left(\frac{f_{i}(\mathbf{y})-f_{i}(\mathbf{x})}{f_{i}^{\max }(\cdot)-f_{i}^{\min }(\cdot)}\right)^{2}}\right\} \tag{17}
\end{equation*}
$$

where $\mathbf{y}$ belongs to the reference solution set $S^{*}$, and $f_{i}(\cdot)$ is the $i$ th objective value, and $f_{i}^{\max }(\cdot)$ and $f_{i}^{\min }(\cdot)$ are the maximum and minimum value of the $i$ th objective in $S$, respectively. If the optimal Pareto front is not

Table 5 Comparisons of MADE_noSL with IMMOGLS2 when considering $f=\left(I_{\text {sum }}, N_{T}\right)$ (same running time)

| Problem | $n, m$ | Tavg | MADE_noSL |  |  |  | IMMOGLS2 |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | ONVG | ONSN | $D I_{R}$ | $A Q$ | ONVG | ONSN | $D I_{R}$ | $A Q$ |
| Car1 | 11,5 | 1.962 | 2.200 | 0.800 | 29.513 | 6448.268 | 3.000 | 2.800 | 0.467 | 6290.819 |
| Car5 | 10,6 | 1.966 | 1.700 | 1.300 | 37.646 | 11102.719 | 3.100 | 3.000 | 1.264 | 10954.321 |
| Car8 | 8,8 | 1.510 | 2.800 | 1.100 | 5.511 | 17006.262 | 2.000 | 2.000 | 0.000 | 16890.764 |
| Rec01 | 20,5 | 4.351 | 3.000 | 0.100 | 53.612 | 1271.101 | 3.500 | 3.400 | 1.228 | 1072.022 |
| Rec05 | 20,5 | 4.859 | 3.300 | 0.100 | 50.277 | 1319.162 | 4.300 | 4.300 | 0.613 | 1150.131 |
| Rec09 | 20,10 | 5.424 | 3.000 | 0.100 | 52.631 | 5485.688 | 4.300 | 4.200 | 0.250 | 4849.659 |
| Rec11 | 20,10 | 6.183 | 3.000 | 0.100 | 58.111 | 4811.464 | 3.900 | 3.900 | 1.359 | 4249.716 |
| Rec15 | 20,15 | 6.445 | 2.300 | 0.200 | 61.855 | 10200.901 | 3.700 | 3.600 | 2.784 | 9262.229 |
| Rec19 | 30,10 | 10.118 | 4.100 | 0.000 | 76.427 | 8432.260 | 4.200 | 4.200 | 0.000 | 6502.370 |
| Rec21 | 30,10 | 10.069 | 3.700 | 0.100 | 69.759 | 8313.107 | 5.100 | 5.100 | 0.907 | 6335.484 |
| Rec25 | 30,15 | 12.623 | 3.900 | 0.100 | 74.005 | 17884.648 | 5.300 | 5.300 | 0.538 | 13973.767 |
| Rec29 | 30,15 | 12.748 | 3.800 | 0.200 | 72.547 | 17526.069 | 4.400 | 4.400 | 2.352 | 13065.492 |
| Rec31 | 50,10 | 24.644 | 4.700 | 0.000 | 96.090 | 15127.245 | 5.400 | 5.400 | 0.000 | 9469.133 |
| Rec35 | 50,10 | 24.452 | 4.700 | 0.000 | 93.376 | 15792.367 | 5.100 | 5.100 | 0.000 | 9987.971 |
| Rec39 | 75,20 | 79.368 | 5.700 | 0.000 | 102.626 | 79810.039 | 6.400 | 6.400 | 0.000 | 50073.733 |
| Ta061 | 100,5 | 89.339 | 6.200 | 0.000 | 108.461 | 9232.315 | 6.600 | 6.600 | 0.000 | 4250.400 |
| Ta065 | 100,5 | 88.289 | 5.700 | 0.000 | 109.956 | 9345.865 | 7.200 | 7.200 | 0.000 | 3969.264 |
| Hel1 | 100,10 | 132.930 | 6.400 | 0.000 | 106.158 | 2858.441 | 7.100 | 7.100 | 0.000 | 1487.329 |
| Ta071 | 100,10 | 128.686 | 6.000 | 0.000 | 108.378 | 32002.972 | 7.300 | 7.300 | 0.000 | 16932.977 |
| Ta075 | 100,10 | 127.942 | 5.700 | 0.000 | 108.395 | 33267.009 | 7.300 | 7.300 | 0.000 | 17244.356 |
| Ta081 | 100,20 | 201.776 | 5.800 | 0.000 | 109.854 | 108575.143 | 7.900 | 7.900 | 0.000 | 63098.259 |
| Ta085 | 100,20 | 205.230 | 5.700 | 0.000 | 107.509 | 103677.036 | 6.100 | 6.100 | 0.000 | 59754.862 |
| Ta091 | 200,10 | 435.360 | 6.300 | 0.000 | 119.863 | 69583.990 | 9.100 | 9.100 | 0.000 | 33434.113 |
| Ta095 | 200,10 | 436.854 | 8.500 | 0.000 | 119.924 | 70300.940 | 10.300 | 10.300 | 0.000 | 33399.257 |
| Ta101 | 200,20 | 660.289 | 8.000 | 0.000 | 119.132 | 214568.344 | 8.600 | 8.600 | 0.000 | 115728.581 |
| Ta105 | 200,20 | 657.980 | 8.100 | 0.000 | 118.778 | 217651.066 | 8.300 | 8.300 | 0.000 | 116083.820 |
| Ta111 | 500,20 | 4976.331 | 12.300 | 0.000 | 127.879 | 575892.948 | 9.700 | 9.700 | 0.000 | 277332.576 |
| Ta115 | 500,20 | 5013.203 | 9.100 | 0.000 | 127.430 | 573640.086 | 8.200 | 8.200 | 0.000 | 280857.271 |
| Average |  |  | 5.204 | 0.150 | 86.632 | 80040.266 | 5.979 | 5.957 | 0.420 | 42417.881 |

known, we will combine these $K$ non-dominated solution sets and select all the non-dominated solutions to form the set $S^{*}$.
The average distance $D I_{R}\left(S_{j}\right)$ is the average of those shortest normalized distances from all the reference solutions to $S_{j}$ (Czyzak and Jaszkiewicz 1998; Knowles and Corne 2002), that is,
$D I_{R}\left(S_{j}\right)=\frac{1}{\left|S^{*}\right|} \sum_{y \in S *} d_{\mathbf{y x}}\left(S_{j}\right)$.

According to (Ishibuchi et al. 2003), $D I_{R}\left(S_{j}\right)$ can be used to evaluate the spread of $S_{j}$ as well as the proximity of $S_{j}$ to the reference set $S^{*}$. Obviously, smaller $D I_{R}\left(S_{j}\right)$ values correspond to a better convergence performance to $S^{*}$. If $D I_{R}\left(S_{j}\right)=0$, all the reference solutions in $S^{*}$ are included in the solution set $S_{j}$.
(5) Average Quality (AQ)

In (Jaszkiewicz 2003), a metric was designed to measure the quality of the solution set, which was originally expressed in the form of weighted Tchebycheff function. But that function may hide certain aspects about the quality of solution set because poor performance with respect to convergence could be compensated by good performance in distribution of solutions. So, diversity indicators of spread and space are added to the formulation to overcome the limitation, and a metric is given by the average value of a scalarized function over a representative sample of weight vectors as follow:

$$
\begin{equation*}
A Q=\sum_{\lambda \in \Lambda} s_{a}\left(\mathbf{f}, \mathbf{z}^{\mathbf{0}}, \lambda, \rho\right) /|\Lambda| \tag{19}
\end{equation*}
$$

Table 6 Comparisons of MADE_noSL with MADE_nospeedup when considering $f=\left(C_{\max }, T_{\max }\right)$ (same running time)

| Problem | $n, m$ | Tavg | MADE_noSL |  |  |  | MADE_nospeedup |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | ONVG | ONSN | $D I_{R}$ | $A Q$ | ONVG | ONSN | $D I_{R}$ | AQ |
| Car1 | 11,5 | 2.201 | 7.800 | 6.900 | 6.851 | 4221.411 | 10.500 | 10.500 | 0.516 | 4177.247 |
| Car5 | 10,6 | 2.005 | 8.400 | 6.500 | 7.228 | 4883.763 | 9.400 | 9.300 | 1.671 | 4761.508 |
| Car8 | 8,8 | 1.532 | 6.000 | 6.000 | 10.587 | 4782.080 | 6.900 | 6.900 | 0.473 | 4761.811 |
| Rec01 | 20,5 | 4.925 | 9.300 | 0.100 | 35.784 | 859.575 | 12.900 | 12.900 | 0.237 | 780.550 |
| Rec05 | 20,5 | 5.130 | 9.400 | 0.200 | 30.339 | 830.390 | 13.300 | 13.300 | 0.223 | 775.708 |
| Rec09 | 20,10 | 6.181 | 8.200 | 0.000 | 40.376 | 1179.760 | 13.100 | 13.100 | 0.000 | 1059.114 |
| Rec11 | 20,10 | 6.386 | 7.400 | 0.000 | 48.547 | 1043.839 | 6.200 | 6.200 | 0.000 | 967.713 |
| Rec15 | 20,15 | 7.046 | 10.400 | 0.000 | 32.445 | 1397.505 | 16.800 | 16.800 | 0.000 | 1287.958 |
| Rec19 | 30,10 | 10.984 | 8.800 | 0.000 | 55.610 | 1812.499 | 10.700 | 10.700 | 0.000 | 1520.520 |
| Rec21 | 30,10 | 10.974 | 9.100 | 0.000 | 71.544 | 1795.125 | 11.500 | 11.500 | 0.000 | 1482.138 |
| Rec25 | 30,15 | 13.400 | 8.900 | 0.000 | 64.226 | 2205.373 | 10.600 | 10.600 | 0.000 | 1905.917 |
| Rec29 | 30,15 | 13.373 | 7.900 | 0.000 | 65.484 | 2095.286 | 12.100 | 12.100 | 0.000 | 1761.073 |
| Rec31 | 50,10 | 26.791 | 9.000 | 0.000 | 85.853 | 3169.323 | 12.700 | 12.700 | 0.000 | 2343.021 |
| Rec35 | 50,10 | 26.622 | 9.300 | 0.000 | 83.835 | 3337.035 | 13.700 | 13.700 | 0.000 | 2418.707 |
| Rec39 | 75,20 | 82.537 | 8.400 | 0.000 | 98.716 | 6841.359 | 9.900 | 9.900 | 0.000 | 4638.389 |
| Ta061 | 100,5 | 93.945 | 10.700 | 0.000 | 103.620 | 5339.674 | 12.400 | 12.400 | 0.000 | 3533.217 |
| Ta065 | 100,5 | 93.514 | 9.500 | 0.000 | 101.229 | 5305.148 | 13.200 | 13.200 | 0.000 | 3385.204 |
| Hel1 | 100,10 | 138.139 | 8.500 | 0.000 | 105.861 | 624.380 | 9.700 | 9.700 | 0.000 | 390.130 |
| Ta071 | 100,10 | 133.516 | 11.000 | 0.000 | 100.326 | 7065.041 | 11.300 | 11.300 | 0.000 | 4475.233 |
| Ta075 | 100,10 | 133.952 | 10.600 | 0.000 | 103.556 | 7047.056 | 13.100 | 13.100 | 0.000 | 4441.916 |
| Ta081 | 100,20 | 201.217 | 10.200 | 0.000 | 101.339 | 9512.533 | 12.800 | 12.800 | 0.000 | 5863.456 |
| Ta085 | 100,20 | 202.622 | 10.900 | 0.000 | 100.241 | 9174.423 | 13.200 | 13.200 | 0.000 | 5787.260 |
| Ta091 | 200,10 | 437.112 | 12.100 | 0.000 | 110.936 | 15435.132 | 13.200 | 13.200 | 0.000 | 8730.636 |
| Ta095 | 200,10 | 436.875 | 7.300 | 0.000 | 112.335 | 15615.812 | 12.700 | 12.700 | 0.000 | 8766.039 |
| Ta101 | 200,20 | 658.878 | 8.800 | 0.000 | 112.893 | 20047.310 | 11.100 | 11.100 | 0.000 | 11370.351 |
| Ta105 | 200,20 | 657.628 | 8.600 | 0.000 | 114.678 | 20647.405 | 10.300 | 10.300 | 0.000 | 11331.889 |
| Ta111 | 500,20 | 5156.385 | 9.100 | 0.000 | 123.361 | 56798.486 | 12.600 | 12.600 | 0.000 | 28300.375 |
| Ta115 | 500,20 | 5172.271 | 12.700 | 0.000 | 116.829 | 57069.386 | 13.100 | 13.100 | 0.000 | 28372.362 |
| Average |  |  | 9.225 | 0.704 | 76.594 | 9647.718 | 11.750 | 11.746 | 0.111 | 5692.480 |

where $s_{a}\left(\mathbf{f}, \mathbf{z}^{\mathbf{0}}, \lambda, \rho\right)=\min _{i}\left\{\max _{j}\left\{\lambda_{j}\left(f_{j}\left(\mathbf{x}_{i}\right)-z_{j}^{0}\right)\right\}+\right.$ $\left.\rho \sum_{j=1}^{w} \lambda_{j}\left(f_{j}\left(\mathbf{x}_{i}\right)-z_{j}^{0}\right)\right\}$, and $f_{j}(\cdot)$ is the $j$ th objective, and $\Lambda=\left\{\lambda=\left(\lambda_{1}, \ldots, \lambda_{w}\right) \mid \lambda_{j} \in\{0,1 / r, 2 / r\right.$, $\left.\ldots, 1\}, \sum_{j=1}^{w} \lambda_{j}=1\right\}$, and $\mathbf{z}^{0}$ is a reference point in the objective space that is set to $(0,0)$ for two-objective problems, and $\rho$ is a sufficiently small number which is set to 0.01 in this paper. Besides, $r$ is a parameter changed as the number of objectives set as $50 . A Q$ can evaluate both the convergence performance and diversity of the solution set. Lower metric value represents better solution set.

### 5.3 Comparisons of MADE_noSL, IMMOGLS2 and MADE_nospeedup

In this subsection, we set the maximum generation of MADE_nospeedup as $t \_$max $=300$ and let MADE_noSL and

IMMOGLS2 run at the same time as MADE_nospeedup. The average running time (second) of each instance, namely Tavg, is given in the corresponding tables.

### 5.3.1 Comparisons of MADE_noSL with IMMOGLS2

In order to test DE's global search ability, we compare MADE_noSL with IMMOGLS2. Simulation results on $f=\left(C_{\max }, T_{\max }\right)$ and $f=\left(I_{\text {sum }}, N_{T}\right)$ can be found in Tables 4 and 5 , respectively.

In Tables 4 and 5, it can be seen from $O N V G$ metric and ONSN metric that IMMOGLS2 can obtain obviously more non-dominated solutions with better convergence performance than MADE_noSL. From $D I_{R}$ metric, it can be seen that the $D I_{R}$ values of IMMOGLS2 are much smaller than those of MADE_noSL. This means that IMMOGLS2 can obtain solutions closer to the optimal Pareto front

Table 7 Comparisons of MADE_noSL with MADE_nospeedup when considering $f=\left(I_{\mathrm{sum}}, N_{T}\right)$ (same running time)

| Problem | $n, m$ | Tavg | MADE_noSL |  |  |  | MADE_nospeedup |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | ONVG | ONSN | $D I_{R}$ | AQ | ONVG | ONSN | $D I_{R}$ | AQ |
| Car1 | 11,5 | 1.962 | 2.200 | 0.600 | 29.681 | 6448.268 | 2.500 | 2.500 | 5.119 | 6266.588 |
| Car5 | 10,6 | 1.966 | 1.700 | 1.300 | 37.089 | 11102.719 | 3.100 | 2.900 | 1.660 | 10947.810 |
| Car8 | 8,8 | 1.510 | 2.800 | 1.100 | 5.511 | 17006.262 | 2.000 | 2.000 | 0.000 | 16890.764 |
| Rec01 | 20,5 | 4.351 | 3.000 | 0.100 | 69.779 | 1271.101 | 3.400 | 3.400 | 0.944 | 1013.571 |
| Rec05 | 20,5 | 4.859 | 3.300 | 0.000 | 61.036 | 1319.162 | 4.300 | 4.300 | 0.000 | 1095.335 |
| Rec09 | 20,10 | 5.424 | 3.000 | 0.000 | 62.541 | 5485.688 | 4.500 | 4.500 | 0.000 | 4671.140 |
| Rec11 | 20,10 | 6.183 | 3.000 | 0.000 | 60.727 | 4811.464 | 4.400 | 4.400 | 0.000 | 4092.068 |
| Rec15 | 20,15 | 6.445 | 2.300 | 0.000 | 68.257 | 10200.901 | 3.300 | 3.300 | 0.000 | 9046.000 |
| Rec19 | 30,10 | 10.118 | 4.100 | 0.000 | 84.596 | 8432.260 | 4.200 | 4.200 | 0.000 | 6193.537 |
| Rec21 | 30,10 | 10.069 | 3.700 | 0.000 | 78.235 | 8313.107 | 4.400 | 4.400 | 0.000 | 6128.207 |
| Rec25 | 30,15 | 12.623 | 3.900 | 0.000 | 79.948 | 17884.648 | 4.500 | 4.500 | 0.000 | 13753.284 |
| Rec29 | 30,15 | 12.748 | 3.800 | 0.000 | 80.605 | 17526.069 | 4.100 | 4.100 | 0.000 | 12636.022 |
| Rec31 | 50,10 | 24.644 | 4.700 | 0.000 | 97.303 | 15127.245 | 4.800 | 4.800 | 0.000 | 9232.426 |
| Rec35 | 50,10 | 24.452 | 4.700 | 0.000 | 94.346 | 15792.367 | 4.700 | 4.700 | 0.000 | 9787.135 |
| Rec39 | 75,20 | 79.368 | 5.700 | 0.000 | 105.474 | 79810.039 | 5.300 | 5.300 | 0.000 | 49885.688 |
| Ta061 | 100,5 | 89.339 | 6.200 | 0.000 | 110.828 | 9232.315 | 5.300 | 5.300 | 0.000 | 4012.488 |
| Ta065 | 100,5 | 88.289 | 5.700 | 0.000 | 114.042 | 9345.865 | 6.400 | 6.400 | 0.000 | 3823.921 |
| Hel1 | 100,10 | 132.930 | 6.400 | 0.000 | 109.835 | 2858.441 | 4.900 | 4.900 | 0.000 | 1432.022 |
| Ta071 | 100,10 | 128.686 | 6.000 | 0.000 | 111.971 | 32002.972 | 5.600 | 5.600 | 0.000 | 16601.863 |
| Ta075 | 100,10 | 127.942 | 5.700 | 0.000 | 111.445 | 33267.009 | 6.100 | 6.100 | 0.000 | 16983.272 |
| Ta081 | 100,20 | 201.776 | 5.800 | 0.000 | 114.387 | 108575.143 | 4.900 | 4.900 | 0.000 | 62198.099 |
| Ta085 | 100,20 | 205.230 | 5.700 | 0.000 | 109.491 | 103677.036 | 5.800 | 5.800 | 0.000 | 59750.541 |
| Ta091 | 200,10 | 435.360 | 6.300 | 0.000 | 124.324 | 69583.990 | 4.600 | 4.600 | 0.000 | 33021.617 |
| Ta095 | 200,10 | 436.854 | 8.500 | 0.000 | 123.447 | 70300.940 | 5.800 | 5.800 | 0.000 | 33146.905 |
| Ta101 | 200,20 | 660.289 | 8.000 | 0.000 | 121.001 | 214568.344 | 5.500 | 5.500 | 0.000 | 115171.246 |
| Ta105 | 200,20 | 657.980 | 8.100 | 0.000 | 119.916 | 217651.066 | 5.600 | 5.600 | 0.000 | 116028.471 |
| Ta111 | 500,20 | 4976.331 | 12.300 | 0.000 | 128.798 | 575892.948 | 5.700 | 5.700 | 0.000 | 269275.363 |
| Ta115 | 500,20 | 4997.203 | 9.100 | 0.000 | 127.558 | 573640.086 | 5.200 | 5.200 | 0.000 | 270432.812 |
| Average |  |  | 5.204 | 0.111 | 90.792 | 80040.266 | 4.675 | 4.668 | 0.276 | 41554.221 |

than MADE_noSL. However, the values of RNDS, ONSN and $D I_{R}$ metrics can not directly reflect the diversity of the solution set. So, we use $A Q$ metric that considers both the convergence performance and diversity for comprehensive comparisons. From Tables 4 and 5, it can be found that the $A Q$ values of IMMOGLS2 are less than those of MADE_noSL. That is to say, the solutions obtained by IMMOGLS2 are closer to the optimal Pareto front than those obtained by MADE_noSL and the solutions obtained by IMMOGLS2 distribute more uniformly and cover more area of the optimal Pareto front.

So it is concluded that DE's global search is not suitable to perform thorough exploitation in the promising regions and has no enough ability to obtain non-dominated solutions with good performance.

### 5.3.2 Comparisons of MADE_noSL with MADE_nospeedup

Next we compare MADE_noSL with MADE_nospeedup to examine the effect of memes on the performance of our MADE_nospeedup. The statistics of performance metrics are given in Tables 6 and 7, respectively.

Tables 6 and 7 show the statistical results produced by MADE_nospeedup are much better than those by MADE_noSL for every instance. As the size of the instance increases, the superiority of MADE_nospeedup over MADE_noSL also increases. This indicates that by embedding the proposed memes into MADE_noSL to enhance exploitation it becomes more efficient and effective to obtain an approximate optimal Pareto set with high quality.

Table 8 Comparisons of MADE_nospeedup with IMMOGLS2 when considering $f=\left(C_{\max }, T_{\max }\right)$ (same running time)

| Problem | Tavg | MADE_nospeedup |  |  |  |  | IMMOGLS2 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | RNDS | ONSN | $D I_{R}$ | TGen | TET | RNDS | ONSN | $D I_{R}$ | TGen | TET |
| Car1 | 2.201 | 0.981 | 10.300 | 0.936 | 300 | 500460 | 0.926 | 8.800 | 4.055 | 1117 | 213050 |
| Car5 | 2.005 | 0.989 | 9.300 | 1.856 | 300 | 457260 | 0.944 | 8.500 | 3.698 | 1048 | 204457 |
| Car8 | 1.532 | 1.000 | 6.900 | 0.000 | 300 | 370860 | 1.000 | 6.900 | 0.000 | 803 | 157865 |
| Rec01 | 4.925 | 0.992 | 12.800 | 0.112 | 300 | 889260 | 0.043 | 0.400 | 18.132 | 2452 | 431492 |
| Rec05 | 5.130 | 0.925 | 12.300 | 0.961 | 300 | 889260 | 0.157 | 2.000 | 15.562 | 2442 | 432015 |
| Rec09 | 6.181 | 0.977 | 12.800 | 0.935 | 300 | 889260 | 0.079 | 1.000 | 17.984 | 2714 | 476850 |
| Rec11 | 6.386 | 0.887 | 5.500 | 7.594 | 300 | 889260 | 0.436 | 4.100 | 12.037 | 2704 | 474582 |
| Rec15 | 7.046 | 0.881 | 14.800 | 0.802 | 300 | 889260 | 0.302 | 3.800 | 10.194 | 2962 | 517233 |
| Rec19 | 10.984 | 0.953 | 10.200 | 1.004 | 300 | 1321260 | 0.097 | 1.200 | 24.439 | 4588 | 777589 |
| Rec21 | 10.974 | 0.991 | 11.400 | 1.108 | 300 | 1321260 | 0.083 | 0.900 | 30.157 | 4594 | 778664 |
| Rec25 | 13.400 | 0.953 | 10.100 | 0.986 | 300 | 1321260 | 0.155 | 1.300 | 29.019 | 4933 | 836617 |
| Rec29 | 13.373 | 0.917 | 11.100 | 3.768 | 300 | 1321260 | 0.291 | 3.400 | 26.349 | 4969 | 836932 |
| Rec31 | 26.791 | 0.945 | 12.000 | 1.293 | 300 | 2185260 | 0.220 | 2.200 | 34.254 | 8934 | 1465672 |
| Rec35 | 26.622 | 0.942 | 12.900 | 1.852 | 300 | 2185260 | 0.217 | 3.500 | 25.536 | 8939 | 1464873 |
| Rec39 | 82.537 | 0.949 | 9.400 | 4.794 | 300 | 3265260 | 0.218 | 3.600 | 41.084 | 16389 | 2644907 |
| Ta061 | 93.945 | 0.992 | 12.300 | 0.358 | 300 | 6026460 | 0.039 | 0.600 | 48.857 | 25031 | 4012639 |
| Ta065 | 93.514 | 1.000 | 13.200 | 0.011 | 300 | 6026460 | 0.008 | 0.100 | 44.404 | 24971 | 4000829 |
| Hel1 | 138.139 | 0.990 | 9.600 | 0.765 | 300 | 6026460 | 0.068 | 0.500 | 50.339 | 27951 | 4488400 |
| Ta071 | 133.516 | 0.991 | 11.200 | 0.612 | 300 | 6026460 | 0.015 | 0.300 | 51.567 | 28021 | 4477938 |
| Ta075 | 133.952 | 1.000 | 13.100 | 0.000 | 300 | 6026460 | 0.000 | 0.000 | 51.771 | 27991 | 4476658 |
| Ta081 | 201.217 | 0.938 | 12.000 | 1.179 | 300 | 6026460 | 0.196 | 3.600 | 41.062 | 30651 | 4899760 |
| Ta085 | 202.622 | 0.970 | 12.800 | 2.348 | 300 | 6026460 | 0.148 | 3.000 | 43.256 | 30611 | 4899094 |
| Ta091 | 437.112 | 0.970 | 12.800 | 0.685 | 300 | 9626460 | 0.087 | 1.300 | 53.196 | 48001 | 7608995 |
| Ta095 | 436.875 | 0.992 | 12.600 | 0.073 | 300 | 9626460 | 0.016 | 0.200 | 44.984 | 48068 | 7617100 |
| Ta101 | 658.878 | 0.982 | 10.900 | 0.321 | 300 | 9626460 | 0.018 | 0.300 | 46.706 | 51801 | 8202919 |
| Ta105 | 657.628 | 1.000 | 10.300 | 0.140 | 300 | 9626460 | 0.074 | 1.300 | 48.894 | 51901 | 8217402 |
| Ta111 | 5156.385 | 1.000 | 12.600 | 0.000 | 300 | 30024060 | 0.000 | 0.000 | 68.139 | 137301 | 21792864 |
| Ta115 | 5172.271 | 1.000 | 13.100 | 0.000 | 300 | 30024060 | 0.000 | 0.000 | 64.011 | 136801 | 21667364 |
| Average |  | 0.968 | 11.368 | 1.232 | 300 | 5694103 | 0.208 | 2.243 | 33.917 | 26382 | 4216956 |

### 5.3.3 Comparisons of MADE_nospeedup and IMMOGLS2

As for multi-objective FSSPs, IMMOGLS2 (Ishibuchi et al. 2003) is famous for its abilities to efficiently find uniformly distributed non-dominated solutions and it outperforms two famous multi-objective evolutionary algorithms, the strength Pareto evolutionary algorithm (SPEA) (Zitzler and Thiele 1999) and the revised non-dominated sorting genetic algorithm (NSGAII) (Deb et al. 2002). Thus, to investigate the search ability of MADE, we compare MADE_nospeedup with IMMOGLS2. The experiment results are illustrated in Tables 8 and 9, where TGen denotes the average generations.

From Tables 8 and 9, it can be found that the values of $R N D S, O N S N$ and $D I_{R}$ produced by MADE_nospeedup are much better than those by IMMOGLS2 for every problem. The TGen values of MADE_nospeedup are equal to 300,
which are much less than those of IMMOGLS2, but the TET value of MADE_nospeedup is obviously larger than that of IMMOGLS2 for each instance. That is, when running at the same time, MADE_nospeedup can explore and exploit more promising regions in the whole solution space than IMMOGLS2. This is the main reason that MADE_nospeedup has relatively good performance.

To better understand the performance of MADE_no speedup on the objectives $f=\left(C_{\max }, T_{\max }\right)$, we plotted the non-dominated solutions of $S_{M A D E \_n o s p e e d u p ~}$ (circle point) and $S_{I M M O G L S 2}$ (star point) and $S_{M A D E \_n o S L}$ (triangle point) for Rec25 in one typical run in Fig. 3. The figure shows that the solutions obtained by MADE_no speedup (circle point) and IMMOGLS2 (star point) are much closer to the optimal Pareto front than those of MADE_noSL (triangle point) and dominate all the MADE_noSL's

Table 9 Comparisons of MADE_nospeedup with IMMOGLS2 when considering $f=\left(I_{\text {sum }}, N_{T}\right)$ (same running time)

| Problem | Tavg | MADE_nospeedup |  |  |  |  | IMMOGLS2 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | RNDS | ONSN | $D I_{R}$ | TGen | TET | RNDS | ONSN | $D I_{R}$ | TGen | TET |
| Car1 | 1.962 | 0.960 | 2.400 | 16.555 | 300 | 500460 | 0.700 | 2.100 | 2.583 | 946 | 204288 |
| Car5 | 1.966 | 0.903 | 2.800 | 11.728 | 300 | 457260 | 0.935 | 2.900 | 7.827 | 915 | 198171 |
| Car8 | 1.510 | 1.000 | 2.000 | 0.000 | 300 | 370860 | 1.000 | 2.000 | 0.000 | 734 | 161790 |
| Rec01 | 4.351 | 1.000 | 3.400 | 2.610 | 300 | 889260 | 0.057 | 0.200 | 46.845 | 2006 | 411119 |
| Rec05 | 4.859 | 0.977 | 4.200 | 0.520 | 300 | 889260 | 0.023 | 0.100 | 33.145 | 2000 | 404462 |
| Rec09 | 5.424 | 0.911 | 4.100 | 1.949 | 300 | 889260 | 0.116 | 0.500 | 24.932 | 2299 | 457297 |
| Rec11 | 6.183 | 0.909 | 4.000 | 1.828 | 300 | 889260 | 0.128 | 0.500 | 22.973 | 2257 | 456910 |
| Rec15 | 6.445 | 0.939 | 3.100 | 3.067 | 300 | 889260 | 0.162 | 0.600 | 25.160 | 2509 | 493028 |
| Rec19 | 10.118 | 0.976 | 4.100 | 0.133 | 300 | 1321260 | 0.048 | 0.200 | 43.740 | 3963 | 735307 |
| Rec21 | 10.069 | 0.955 | 4.200 | 1.782 | 300 | 1321260 | 0.059 | 0.300 | 30.721 | 3934 | 735933 |
| Rec25 | 12.623 | 0.911 | 4.100 | 2.852 | 300 | 1321260 | 0.132 | 0.700 | 24.013 | 4348 | 797826 |
| Rec29 | 12.748 | 0.976 | 4.000 | 1.348 | 300 | 1321260 | 0.045 | 0.200 | 31.889 | 4357 | 803212 |
| Rec31 | 24.644 | 0.813 | 3.900 | 4.260 | 300 | 2185260 | 0.204 | 1.100 | 26.574 | 7879 | 1372958 |
| Rec35 | 24.452 | 0.702 | 3.300 | 7.252 | 300 | 2185260 | 0.333 | 1.700 | 21.725 | 7841 | 1365446 |
| Rec39 | 79.368 | 0.887 | 4.700 | 6.583 | 300 | 3265260 | 0.281 | 1.800 | 25.932 | 15339 | 2544527 |
| Ta061 | 89.339 | 1.000 | 5.300 | 0.000 | 300 | 6026460 | 0.000 | 0.000 | 45.715 | 23581 | 3932148 |
| Ta065 | 88.289 | 0.984 | 6.300 | 0.807 | 300 | 6026460 | 0.056 | 0.400 | 39.465 | 23411 | 3908370 |
| Hell | 132.930 | 1.000 | 4.900 | 0.000 | 300 | 6026460 | 0.000 | 0.000 | 49.604 | 26721 | 4465173 |
| Ta071 | 128.686 | 0.982 | 5.500 | 1.853 | 300 | 6026460 | 0.082 | 0.600 | 32.793 | 26781 | 4417008 |
| Ta075 | 127.942 | 0.984 | 6.000 | 2.812 | 300 | 6026460 | 0.151 | 1.100 | 34.735 | 26721 | 4407456 |
| Ta081 | 201.776 | 0.918 | 4.500 | 3.951 | 300 | 6026460 | 0.165 | 1.300 | 40.698 | 29801 | 4854814 |
| Ta085 | 205.230 | 0.793 | 4.600 | 8.402 | 300 | 6026460 | 0.426 | 2.600 | 29.525 | 29841 | 4866382 |
| Ta091 | 435.360 | 1.000 | 4.600 | 3.085 | 300 | 9626460 | 0.033 | 0.300 | 50.849 | 46868 | 7560615 |
| Ta095 | 436.854 | 0.914 | 5.300 | 10.268 | 300 | 9626460 | 0.223 | 2.300 | 40.336 | 46834 | 7555082 |
| Ta101 | 660.289 | 0.927 | 5.100 | 19.363 | 300 | 9626460 | 0.349 | 3.000 | 31.199 | 50668 | 8109910 |
| Ta105 | 657.980 | 0.893 | 5.000 | 14.450 | 300 | 9626460 | 0.422 | 3.500 | 28.167 | 50868 | 8140486 |
| Ta111 | 4976.331 | 1.000 | 5.700 | 0.000 | 300 | 30024060 | 0.000 | 0.000 | 80.053 | 136601 | 21606733 |
| Ta115 | 4997.203 | 1.000 | 5.200 | 0.000 | 300 | 30024060 | 0.000 | 0.000 | 88.523 | 135951 | 21537702 |
| Average |  | 0.936 | 4.368 | 4.552 | 300 | 5694103 | 0.219 | 1.071 | 34.276 | 25571 | 4160862 |

solutions. Furthermore, it can be easily seen that MADE_no speedup performs better than IMMOGLS2. The corresponding values of performance metrics are reported in Table 10. Experiment results for other problems are similar.

Moreover, typical results of a replication for the three algorithms based on the objectives $f=\left(I_{\text {sum }}, N_{T}\right)$ and the benchmark Rec 11 are shown in Fig. 4. And the corresponding values of the performance metrics are given in Table 11. As can be seen from Fig. 4 and Table 11, MADE_nospeedup's solutions (circle point) dominate all the IMMOGLS2's solutions (star point) and all the MADE_noSL's solutions (triangle point). As for other problems, conclusions are similar.

To sum up, MADE_nospeedup is a more effective and efficient multi-objective optimization algorithm than IMMOGLS2 and MADE_noSL.

### 5.4 Comparisons of MADE with MADE_nospeedup

To further show the effectiveness of MADE by incorporating speed-up computing method into MADE_nospeedup, we compare MADE with MADE_nospeedup. In MADE_no speedup, both ( $C_{\max }, T_{\max }$ ) and ( $I_{\text {sum }}, N_{T}$ ) can be computed in $O(n m)$. And in MADE, where speed-up computing method is adopted, both the CC of computing $\left(C_{\max }, T_{\max }\right.$ ) and that of computing $\left(I_{\text {sum }}, N_{T}\right)$ are reduced to $O(n)$. Let TCC_MADE_nospeedup $(O F 1, O F 2)$ denote the total CC of calculating two objective functions, i.e., $O F 1$ and $O F 2$, in MADE_nospeedup, TCC_MADE (OF1, OF2) denote the total CC of calculating $O F 1$ and $O F 2$ in MADE. When MADE and MADE_nospeedup run at the same TET (i.e., $K_{1}$, times), TCC_MADE( $\left.C_{\max }, T_{\max }\right)$ can be reduced

Fig. 3 Non-dominated solutions of MADE_nospeedup and IMMOGLS2 and MADE_noSL $\left(C_{\max }, T_{\max }\right)$


Table 10 The values of performance metrics corresponding to Fig. 3

| $\left(C_{\max }, T_{\max }\right)$ | MADE_noSL vs IMMOGLS2 |  | MADE_noSL vs. MADE_nospeedup |  | MADE_nospeedup vs. IMMOGLS2 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | MADE_noSL | IMMOGLS2 | MADE_noSL | MADE _nospeedup | MADE _nospeedup | IMMOGLS2 |
| RNDS | 0.000 | 1.000 | 0.000 | 1.000 | 1.000 | 0.133 |
| ONVG | 11.000 | 15.000 | 11.000 | 10.000 | 10.000 | 15.000 |
| ONSN | 0.000 | 15.000 | 0.000 | 10.000 | 10.000 | 2.000 |
| $D I_{R}$ | 58.963 | 0.000 | 66.553 | 0.000 | 0.257 | 22.003 |
| AQ | 2211.807 | 1930.320 | 2211.807 | 1904.625 | 1904.625 | 1930.320 |

Fig. 4 Non-dominated solutions of MADE_nospeedup and IMMOGLS2 and $\operatorname{MADE} \_$noSL $\left(I_{\text {sum }}, N_{\mathrm{T}}\right)$


Table 11 The values of performance metrics corresponding to Fig. 4

| $\left(I_{\text {sum }}, N_{T}\right)$ | MADE_noSL vs IMMOGLS2 |  | MADE_noSL vs. MADE_nospeedup |  | MADE_nospeedup vs. IMMOGLS2 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | MADE_noSL | IMMOGLS2 | MADE_noSL | MADE _nospeedup | MADE _nospeedup | IMMOGLS2 |
| RNDS | 0.000 | 1.000 | 0.000 | 1.000 | 1.000 | 0.000 |
| ONVG | 3.000 | 3.000 | 3.000 | 5.000 | 5.000 | 3.000 |
| ONSN | 0.000 | 3.000 | 0.000 | 5.000 | 5.000 | 0.000 |
| $D I_{R}$ | 53.344 | 0.000 | 50.918 | 0.000 | 0.000 | 19.518 |
| AQ | 4806.019 | 4221.229 | 4806.019 | 4078.764 | 4078.764 | 4221.229 |

Table 12 Comparisons of MADE with MADE_nospeedup when considering $f=\left(C_{\max }, T_{\max }\right)$ (same running time)

| Problem | MADE_nospeedup |  |  |  |  | MADE |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | RNDS | ONSN | $D I_{R}$ | AQ | TET | RNDS | ONSN | $D I_{R}$ | AQ | TET |
| Car1 | 1.000 | 10.900 | 1.417 | 4170.667 | 500460 | 0.991 | 11.200 | 0.597 | 4170.453 | 999526 |
| Car5 | 0.968 | 9.200 | 1.973 | 4749.634 | 457260 | 0.980 | 9.600 | 0.577 | 4750.289 | 932900 |
| Car8 | 1.000 | 7.000 | 0.000 | 4761.173 | 370860 | 1.000 | 7.000 | 0.000 | 4761.173 | 810011 |
| Rec01 | 0.528 | 6.700 | 4.362 | 782.824 | 889260 | 0.836 | 11.700 | 0.954 | 779.693 | 1768382 |
| Rec05 | 0.419 | 5.400 | 5.020 | 778.069 | 889260 | 0.800 | 10.400 | 1.860 | 776.328 | 1705842 |
| Rec09 | 0.310 | 4.000 | 5.008 | 1062.080 | 889260 | 0.866 | 13.600 | 0.846 | 1056.934 | 2164076 |
| Rec11 | 0.719 | 4.600 | 9.258 | 968.124 | 889260 | 0.975 | 7.900 | 1.323 | 963.206 | 2192827 |
| Rec15 | 0.439 | 6.800 | 3.009 | 1286.751 | 889260 | 0.880 | 16.900 | 0.369 | 1284.291 | 2697004 |
| Rec19 | 0.274 | 3.100 | 6.886 | 1519.210 | 1321260 | 0.795 | 8.900 | 1.702 | 1511.279 | 3030012 |
| Rec21 | 0.364 | 3.900 | 7.574 | 1483.129 | 1321260 | 0.738 | 10.400 | 2.333 | 1475.876 | 3106201 |
| Rec25 | 0.240 | 2.300 | 10.286 | 1906.478 | 1321260 | 0.845 | 9.800 | 1.948 | 1893.397 | 3865451 |
| Rec29 | 0.391 | 4.500 | 5.262 | 1757.966 | 1321260 | 0.690 | 10.900 | 1.588 | 1760.117 | 3912574 |
| Rec31 | 0.330 | 3.800 | 6.619 | 2343.239 | 2185260 | 0.779 | 11.300 | 1.765 | 2336.331 | 5401146 |
| Rec35 | 0.496 | 6.500 | 4.111 | 2409.761 | 2185260 | 0.698 | 11.100 | 1.771 | 2400.081 | 4875970 |
| Rec39 | 0.144 | 1.700 | 10.528 | 4646.397 | 3265260 | 0.932 | 12.400 | 0.857 | 4618.432 | 12509041 |
| Ta061 | 0.397 | 4.800 | 7.216 | 3536.685 | 6026460 | 0.780 | 9.200 | 4.646 | 3527.528 | 13748287 |
| Ta065 | 0.220 | 2.700 | 8.257 | 3393.402 | 6026460 | 0.844 | 11.900 | 2.092 | 3378.404 | 13947158 |
| Hel1 | 0.152 | 1.400 | 11.088 | 390.267 | 6026460 | 0.890 | 9.700 | 0.947 | 387.593 | 18515170 |
| Ta071 | 0.246 | 3.300 | 7.482 | 4450.146 | 6026460 | 0.835 | 11.600 | 1.920 | 4430.940 | 19728485 |
| Ta075 | 0.235 | 2.300 | 10.354 | 4438.651 | 6026460 | 0.831 | 10.800 | 1.453 | 4410.699 | 17121062 |
| Ta081 | 0.167 | 2.100 | 9.028 | 5873.568 | 6026460 | 0.922 | 14.100 | 0.992 | 5809.913 | 29485226 |
| Ta085 | 0.153 | 1.700 | 11.638 | 5800.144 | 6026460 | 0.929 | 14.500 | 1.457 | 5734.586 | 29774494 |
| Ta091 | 0.141 | 2.000 | 8.680 | 8752.709 | 9626460 | 0.989 | 17.300 | 1.542 | 8638.003 | 35355688 |
| Ta095 | 0.219 | 2.800 | 10.126 | 8727.668 | 9626460 | 0.920 | 16.100 | 1.548 | 8606.164 | 35179204 |
| Ta101 | 0.165 | 2.000 | 12.579 | 11207.666 | 9626460 | 0.936 | 13.200 | 0.685 | 11024.192 | 48821952 |
| Ta105 | 0.091 | 0.900 | 12.432 | 11398.121 | 9626460 | 0.938 | 15.100 | 0.276 | 11256.865 | 51249944 |
| Ta111 | 0.112 | 1.600 | 31.764 | 28276.972 | 30024060 | 0.910 | 15.100 | 26.069 | 27733.851 | 154273380 |
| Ta115 | 0.095 | 1.100 | 14.956 | 28277.364 | 30024060 | 1.000 | 13.400 | 1.533 | 27627.245 | 150170100 |
| Average | 0.358 | 3.896 | 8.461 | 5683.888 | 5694103 | 0.876 | 11.968 | 2.273 | 5610.852 | 23833611 |

from $O\left(K_{1} n m\right)$ of TCC_MADE_nospeedup $\left(C_{\max }\right.$, $\left.T_{\max }\right)$ to $O\left(K_{1} n\right)$ and TCC_MADE $\left(I_{\text {sum }}, N_{T}\right)$ can be reduced from $O\left(K_{1} \mathrm{~nm}\right)$ of TCC_MADE_nospeedup $\left(I_{\text {sum }}, N_{T}\right)$ to $O\left(K_{1} n\right)$.

### 5.4.1 Comparisons based on a fixed computational budget

Firstly, we set the maximum generation of MADE_nospeedup as $t \_\max =300$ and let MADE run at the same time as

Table 13 Comparisons of MADE with MADE_nospeedup when considering $f=\left(I_{\text {sum }}, N_{T}\right)$ (same running time)

| Problem | MADE_nospeedup |  |  |  |  | MADE |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | RNDS | ONSN | $D I_{R}$ | AQ | TET | RNDS | ONSN | $D I_{R}$ | $A Q$ | TET |
| Car1 | 0.913 | 2.100 | 8.356 | 6266.591 | 500460 | 1.000 | 2.500 | 3.490 | 6266.589 | 711295 |
| Car5 | 0.909 | 3.000 | 1.809 | 10945.839 | 457260 | 0.941 | 3.200 | 0.250 | 10941.900 | 601583 |
| Car8 | 1.000 | 2.000 | 0.000 | 16890.764 | 370860 | 1.000 | 2.000 | 0.000 | 16890.764 | 547114 |
| Rec01 | 0.568 | 2.100 | 13.687 | 1009.662 | 889260 | 0.854 | 3.500 | 5.945 | 1003.196 | 1423373 |
| Rec05 | 0.286 | 1.200 | 9.499 | 1095.613 | 889260 | 0.864 | 3.800 | 2.122 | 1086.271 | 1267170 |
| Rec09 | 0.317 | 1.300 | 8.305 | 4668.916 | 889260 | 0.837 | 4.100 | 1.420 | 4650.637 | 1938220 |
| Rec11 | 0.553 | 2.100 | 7.588 | 4106.237 | 889260 | 0.756 | 3.100 | 3.642 | 4078.965 | 1566238 |
| Rec15 | 0.667 | 2.000 | 6.783 | 9033.474 | 889260 | 0.903 | 2.800 | 1.575 | 9033.122 | 2234323 |
| Rec19 | 0.147 | 0.500 | 21.763 | 6203.915 | 1321260 | 0.919 | 3.400 | 4.493 | 6155.382 | 3511369 |
| Rec21 | 0.333 | 1.400 | 12.939 | 6132.472 | 1321260 | 0.750 | 3.600 | 4.877 | 6081.009 | 3292931 |
| Rec25 | 0.289 | 1.300 | 17.157 | 13729.679 | 1321260 | 0.784 | 4.000 | 1.787 | 13600.439 | 4099744 |
| Rec29 | 0.300 | 1.200 | 14.968 | 12661.646 | 1321260 | 0.778 | 3.500 | 4.321 | 12478.479 | 4130572 |
| Rec31 | 0.268 | 1.100 | 15.538 | 9193.316 | 2185260 | 0.783 | 4.700 | 2.385 | 9107.949 | 6704254 |
| Rec35 | 0.298 | 1.400 | 15.193 | 9830.845 | 2185260 | 0.750 | 4.500 | 3.489 | 9700.398 | 6662006 |
| Rec39 | 0.091 | 0.300 | 23.802 | 49939.014 | 3265260 | 0.902 | 5.500 | 0.850 | 49022.620 | 19307188 |
| Ta061 | 0.415 | 2.200 | 14.964 | 4045.913 | 6026460 | 0.815 | 5.300 | 4.521 | 3981.624 | 19917312 |
| Ta065 | 0.278 | 1.000 | 19.572 | 3800.234 | 6026460 | 0.786 | 4.400 | 4.447 | 3758.555 | 20475758 |
| Hel1 | 0.213 | 1.000 | 24.682 | 1437.772 | 6026460 | 0.796 | 4.300 | 2.923 | 1419.663 | 25879430 |
| Ta071 | 0.118 | 0.600 | 20.911 | 16602.528 | 6026460 | 0.902 | 5.500 | 0.693 | 16342.738 | 29083466 |
| Ta075 | 0.109 | 0.700 | 18.269 | 17009.129 | 6026460 | 0.873 | 6.200 | 0.484 | 16814.526 | 23350351 |
| Ta081 | 0.125 | 0.500 | 20.528 | 62180.878 | 6026460 | 0.955 | 6.400 | 0.784 | 61269.480 | 40545679 |
| Ta085 | 0.143 | 0.700 | 19.700 | 59635.511 | 6026460 | 0.935 | 7.200 | 0.414 | 58806.785 | 40891193 |
| Ta091 | 0.156 | 1.000 | 17.354 | 32946.528 | 9626460 | 0.947 | 7.100 | 1.356 | 32470.454 | 44078276 |
| Ta095 | 0.000 | 0.000 | 22.980 | 33211.048 | 9626460 | 1.000 | 7.200 | 0.000 | 32627.303 | 39976360 |
| Ta101 | 0.090 | 0.700 | 22.972 | 115092.964 | 9626460 | 0.973 | 7.100 | 1.906 | 113810.132 | 62357740 |
| Ta105 | 0.094 | 0.500 | 24.442 | 115944.076 | 9626460 | 0.958 | 6.800 | 0.895 | 114933.432 | 67352772 |
| Ta111 | 0.000 | 0.000 | 39.002 | 268005.032 | 30024060 | 1.000 | 7.300 | 0.000 | 265567.733 | 189251340 |
| Ta115 | 0.000 | 0.000 | 35.874 | 270647.158 | 30024060 | 1.000 | 8.400 | 0.000 | 266637.278 | 189301380 |
| Average | 0.310 | 1.139 | 17.094 | 41509.527 | 5694103 | 0.884 | 4.907 | 2.110 | 41019.194 | 30373516 |

MADE_nospeedup. Simulation results on $f=\left(C_{\max }, T_{\max }\right)$ and $f=\left(I_{\text {sum }}, N_{T}\right)$ are shown in Tables 12 and 13 , respectively.

From Table 12, it can be seen that the average TET of MADE is 4.2 times larger than that of MADE_nospeedup, which testifies that the evaluation time of solution can be significantly reduced by the speed-up computing method. Furthermore, all performance metrics values of MADE are obviously better than those of MADE_nospeedup. This means that, under the same running time, MADE can spend more time in executing search operation in the solution space, which is helpful to obtain the optimal Pareto front. Similar conclusion can be drawn from Table 13.

### 5.4.2 Comparisons with the same running generation

Secondly, we let MADE and MADE_nospeedup run the same generation (i.e., $\left.t \_\max =300\right)$. Test results on $f=\left(C_{\max }\right.$, $\left.T_{\max }\right)$ and $f=\left(I_{\text {sum }}, N_{T}\right)$ are illustrated in Tables 14 and 15 respectively, where Tavg denotes the average CPU time (second) of ten runs.

It is shown from Table 14 that the differences between performance metrics values of MADE and those of MADE_nospeedup are quite minor. That is to say, when running same generation, MADE and MADE_nospeedup can obtain similar non-dominated solutions. However, especially for the large problems, the Tavg of MADE is obviously

Table 14 Comparisons of MADE with MADE_nospeedup when considering $f=\left(C_{\max }, T_{\max }\right)$ (same running generation)

| Problem | MADE_nospeedup |  |  |  |  | MADE |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | RNDS | ONSN | $D I_{R}$ | AQ | Tavg | RNDS | ONSN | $D I_{R}$ | $A Q$ | Tavg |
| Car1 | 0.972 | 10.400 | 1.243 | 4177.153 | 2.423 | 1.000 | 10.900 | 0.308 | 4168.629 | 1.586 |
| Car5 | 0.979 | 9.200 | 1.107 | 4766.167 | 1.930 | 0.989 | 9.200 | 1.605 | 4786.309 | 1.275 |
| Car8 | 1.000 | 6.800 | 2.005 | 4764.539 | 1.494 | 1.000 | 6.900 | 1.059 | 4763.264 | 0.936 |
| Rec01 | 0.634 | 8.500 | 3.055 | 781.260 | 4.561 | 0.629 | 9.000 | 2.779 | 783.343 | 2.773 |
| Rec05 | 0.602 | 8.000 | 2.744 | 776.329 | 5.253 | 0.606 | 7.700 | 3.718 | 777.120 | 3.431 |
| Rec09 | 0.645 | 8.900 | 2.974 | 1060.886 | 5.805 | 0.624 | 8.300 | 2.876 | 1061.066 | 2.922 |
| Rec11 | 0.933 | 5.600 | 5.827 | 966.583 | 6.659 | 0.788 | 5.200 | 5.337 | 966.331 | 2.803 |
| Rec15 | 0.573 | 9.800 | 2.027 | 1287.307 | 6.627 | 0.614 | 10.200 | 2.153 | 1286.758 | 2.704 |
| Rec19 | 0.648 | 6.800 | 4.428 | 1520.098 | 10.300 | 0.524 | 6.500 | 3.905 | 1524.042 | 4.139 |
| Rec21 | 0.544 | 6.200 | 4.770 | 1484.482 | 10.585 | 0.560 | 7.000 | 4.892 | 1485.308 | 4.453 |
| Rec25 | 0.613 | 6.500 | 4.362 | 1902.208 | 12.775 | 0.557 | 5.400 | 5.176 | 1906.549 | 4.409 |
| Rec29 | 0.545 | 6.100 | 4.851 | 1769.807 | 12.951 | 0.570 | 6.900 | 4.021 | 1766.794 | 4.481 |
| Rec31 | 0.614 | 7.000 | 3.511 | 2346.677 | 25.820 | 0.481 | 6.300 | 4.295 | 2338.303 | 9.719 |
| Rec35 | 0.626 | 7.700 | 3.522 | 2418.355 | 26.020 | 0.526 | 7.000 | 3.217 | 2414.257 | 10.059 |
| Rec39 | 0.512 | 6.300 | 4.175 | 4645.296 | 80.105 | 0.576 | 7.600 | 5.106 | 4649.754 | 17.308 |
| Ta061 | 0.464 | 5.200 | 5.776 | 3533.974 | 94.277 | 0.648 | 7.000 | 4.913 | 3531.098 | 52.614 |
| Ta065 | 0.521 | 6.200 | 5.993 | 3395.795 | 93.497 | 0.635 | 8.000 | 3.750 | 3381.977 | 52.511 |
| Hel1 | 0.793 | 6.900 | 4.921 | 389.757 | 137.488 | 0.387 | 4.100 | 8.140 | 391.299 | 52.589 |
| Ta071 | 0.652 | 7.500 | 5.035 | 4455.661 | 132.941 | 0.475 | 5.800 | 5.292 | 4466.872 | 52.614 |
| Ta075 | 0.569 | 6.600 | 6.409 | 4446.235 | 132.933 | 0.543 | 6.300 | 5.075 | 4426.617 | 52.760 |
| Ta081 | 0.433 | 5.200 | 6.084 | 5882.187 | 199.245 | 0.679 | 8.900 | 3.690 | 5868.730 | 54.208 |
| Ta085 | 0.535 | 6.100 | 5.386 | 5809.396 | 201.292 | 0.577 | 7.100 | 4.779 | 5813.518 | 57.378 |
| Ta091 | 0.565 | 7.000 | 4.319 | 8730.569 | 438.911 | 0.483 | 6.900 | 4.245 | 8739.799 | 119.537 |
| Ta095 | 0.652 | 7.500 | 4.821 | 8705.978 | 437.271 | 0.523 | 5.800 | 6.589 | 8736.021 | 119.490 |
| Ta101 | 0.521 | 5.000 | 8.143 | 11375.480 | 658.766 | 0.639 | 7.600 | 3.184 | 11254.455 | 128.914 |
| Ta105 | 0.505 | 5.300 | 7.768 | 11446.594 | 649.971 | 0.562 | 6.800 | 6.091 | 11419.405 | 122.112 |
| Ta111 | 0.644 | 8.700 | 7.521 | 28718.063 | 5195.164 | 0.525 | 6.400 | 10.709 | 28962.025 | 1026.930 |
| Ta115 | 0.551 | 7.600 | 4.825 | 28418.446 | 5209.621 | 0.607 | 8.200 | 3.243 | 28242.137 | 1057.640 |
| Average | 0.637 | 7.093 | 4.557 | 5713.403 | 492.667 | 0.619 | 7.250 | 4.291 | 5711.135 | 107.939 |

smaller than that of MADE_nospeedup. The average Tavg of MADE is 4.6 times smaller than that of MADE_nospeedup. This is very meaningful for real-time applications and dynamic scheduling, in which achieving satisfied solutions within a short time is critical. Similar conclusion also can be drawn from Table 15.

In conclusion, MADE is the most effective and efficient multi-objective optimization algorithm among the four compared algorithms.

## 6 Conclusions

In this article, a memetic algorithm based on DE (MADE) is presented for solving multi-objective no-waiting flow-shop scheduling problems (MNFSSPs). In order to apply DE for

FSSPs problems, we proposed a LOV rule to map the continuous values of an individual into a job permutation of FSSPs. We also adopted the concept of Pareto dominance to handle the updating of solutions in multi-objective sense. In our proposed algorithm, not only did DE-based wide scatter search be utilized to find enough promising regions, but also several problem-specific memes were designed to perform a thorough and deep search in these promising regions. Moreover, a speed-up computing method was developed to reduce the computing complexity of solution evaluation, that is, we considered the improvements of both the effectiveness of searching solutions and the efficiency of evaluating solutions. Simulation results and comparisons based on a set of benchmarks demonstrated the effectiveness and efficiency of MADE.

Table 15 Comparisons of MADE with MADE_nospeedup when considering $f=\left(I_{\text {sum }}, N_{T}\right)$ (same running generation)

| Problem | MADE_nospeedup |  |  |  |  | MADE |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | RNDS | ONSN | $D I_{R}$ | AQ | Tavg | RNDS | ONSN | $D I_{R}$ | $A Q$ | Tavg |
| Car1 | 0.960 | 2.400 | 7.185 | 6266.589 | 2.291 | 0.958 | 2.300 | 11.850 | 6266.591 | 1.470 |
| Car5 | 0.935 | 2.900 | 10.472 | 10949.779 | 2.191 | 0.917 | 3.300 | 1.800 | 10937.960 | 1.498 |
| Car8 | 1.000 | 2.000 | 0.000 | 16890.764 | 1.430 | 1.000 | 2.000 | 0.000 | 16890.764 | 0.884 |
| Rec01 | 0.800 | 2.800 | 7.809 | 1011.980 | 4.442 | 0.667 | 2.600 | 7.243 | 1005.925 | 2.592 |
| Rec05 | 0.548 | 2.300 | 4.843 | 1096.169 | 5.500 | 0.675 | 2.700 | 5.118 | 1097.177 | 3.639 |
| Rec09 | 0.643 | 2.700 | 7.992 | 4671.443 | 5.658 | 0.683 | 2.800 | 6.155 | 4671.642 | 2.625 |
| Rec11 | 0.639 | 2.300 | 11.080 | 4098.513 | 6.620 | 0.561 | 2.300 | 5.100 | 4113.106 | 2.511 |
| Rec15 | 0.606 | 2.000 | 6.117 | 9036.557 | 6.673 | 0.933 | 2.800 | 8.205 | 9036.561 | 2.525 |
| Rec19 | 0.538 | 2.100 | 9.718 | 6194.875 | 10.233 | 0.516 | 1.600 | 7.939 | 6203.557 | 3.678 |
| Rec21 | 0.366 | 1.500 | 10.803 | 6151.922 | 10.239 | 0.632 | 2.400 | 7.518 | 6122.275 | 3.822 |
| Rec25 | 0.614 | 2.700 | 7.330 | 13695.844 | 12.958 | 0.455 | 2.000 | 8.641 | 13733.615 | 3.981 |
| Rec29 | 0.558 | 2.400 | 7.006 | 12627.610 | 13.077 | 0.500 | 2.100 | 9.687 | 12638.520 | 4.028 |
| Rec31 | 0.500 | 2.300 | 11.894 | 9267.815 | 25.277 | 0.630 | 3.400 | 8.807 | 9254.565 | 7.748 |
| Rec35 | 0.327 | 1.800 | 9.283 | 9775.352 | 25.221 | 0.744 | 3.200 | 7.308 | 9797.619 | 7.665 |
| Rec39 | 0.554 | 3.100 | 13.729 | 50041.328 | 81.525 | 0.564 | 3.100 | 8.614 | 50009.214 | 13.617 |
| Ta061 | 0.589 | 3.300 | 11.598 | 4072.539 | 89.651 | 0.600 | 3.300 | 7.624 | 4026.334 | 29.163 |
| Ta065 | 0.611 | 3.300 | 7.880 | 3787.457 | 88.714 | 0.540 | 2.700 | 10.576 | 3826.838 | 29.123 |
| Hell | 0.688 | 3.300 | 7.388 | 1432.918 | 133.989 | 0.403 | 2.500 | 12.623 | 1438.734 | 29.052 |
| Ta071 | 0.633 | 3.800 | 7.489 | 16539.856 | 129.081 | 0.421 | 2.400 | 11.177 | 16537.319 | 29.192 |
| Ta075 | 0.571 | 3.200 | 9.345 | 16903.369 | 128.408 | 0.490 | 2.500 | 11.180 | 16986.848 | 29.494 |
| Ta081 | 0.333 | 2.200 | 11.707 | 62325.617 | 203.800 | 0.786 | 4.400 | 5.873 | 61905.444 | 35.497 |
| Ta085 | 0.509 | 2.800 | 7.525 | 59573.442 | 211.613 | 0.541 | 3.300 | 8.696 | 59500.372 | 40.523 |
| Ta091 | 0.640 | 3.200 | 10.347 | 32932.648 | 433.299 | 0.525 | 3.100 | 16.526 | 33085.582 | 93.883 |
| Ta095 | 0.672 | 4.300 | 6.338 | 33023.507 | 444.964 | 0.408 | 2.900 | 15.918 | 32944.996 | 106.859 |
| Ta101 | 0.433 | 2.900 | 7.993 | 114888.203 | 664.591 | 0.644 | 4.700 | 5.738 | 115302.791 | 102.898 |
| Ta105 | 0.667 | 3.800 | 12.361 | 116246.703 | 653.510 | 0.492 | 3.200 | 7.842 | 115722.781 | 93.365 |
| Ta111 | 0.451 | 3.200 | 13.215 | 268461.025 | 4942.188 | 0.346 | 2.700 | 10.363 | 268620.583 | 661.523 |
| Ta115 | 0.539 | 4.100 | 3.438 | 271268.743 | 4961.109 | 0.444 | 3.200 | 10.066 | 270881.992 | 691.407 |
| Average | 0.604 | 2.811 | 8.639 | 41544.020 | 474.938 | 0.610 | 2.839 | 8.507 | 41519.989 | 72.652 |

To the best of our knowledge, this is the first paper to apply the standard DE for multi-objective no-wait flow-shop scheduling problems. In our future research, we will propose some adaptive strategies to improve the efficiency of MADE, and extend MADE to solve other kinds of scheduling problems, such as stochastic scheduling.

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## Appendix 1 : The algorithm to calculate $M D\left(\pi_{j-1}, \pi_{j}\right)$

Step 1: Set $p_{1}=0, p_{2}=0$ and $k=2$;
Step 2: Do
$p_{1}=p_{1}+p\left(\pi_{j-1}, k\right) ;$
$p_{2}=p_{2}+p\left(\pi_{j}, k-1\right) ;$
If $k=2$ then
$\max _{-} p=p_{1}-p_{2}$
Else
$\max p=\max \left\{\max p, p_{1}-p_{2}\right\}$;
$k=k+1$;
While $k \leq m$;
Step 3: $M D\left(\pi_{j-1}, \pi_{j}\right)=p\left(\pi_{j-1}, 1\right)+\max \left\{0, \max _{\_} p\right\}$;

## Appendix 2 : The algorithm to calculate

$\sum_{k=1}^{m} \sum_{y=1}^{k} p\left(\pi_{n}, y\right)$
Step 1: Set $p_{\text {sum }}=0, p=0$ and $k=1$;
Step 2: Do

$$
\begin{aligned}
& p=p+p\left(\pi_{n}, k\right) ; \quad / / p=\sum_{y=1}^{k} p\left(\pi_{n}, y\right) \\
& p_{\text {sum }}=p_{\text {sum }}+p ; \\
& k=k+1 ; \\
& \text { While } k \leq m ;
\end{aligned}
$$

Remark In Step 2, $p$ is used to save the current value of $\sum_{y=1}^{k} p\left(\pi_{n}, y\right)$ in each loop. If the equation $p=p+p\left(\pi_{n}, k\right)$ is replaced with the equation $p=\sum_{y=1}^{k} p\left(\pi_{n}, y\right)$, the CC of $\sum_{k=1}^{m} \sum_{y=1}^{k} p\left(\pi_{n}, y\right)$ will rise from $O(m)$ to $O\left(m^{2}\right)$. For the purpose of reducing the computing complexity, the equation $p=p+p\left(\pi_{n}, k\right)$ is adopted in Step 2.

## Appendix 3 : The algorithm to calculate <br> $$
C\left(\pi_{j}, m\right) \quad\left(\pi_{j} \in\{1, \ldots, n\}\right)
$$

Step 1: Calculate $C\left(\pi_{1}, m\right)=\sum_{y=1}^{m} p\left(\pi_{1}, y\right)$ and set $M D \_$sum $=0$;
Step 2: Set $j=2$ and $p=0$;
Do
$M D \_$sum $=M D \_$sum $+M D\left(\pi_{j-1}, \pi_{j}\right)$;
$C\left(\pi_{j}, m\right)=M D_{-}$sum $+P_{\text {sum }}\left(\pi_{j}\right) ;$
$j=j+1$;
While $j \leq n$;

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